

Static and Dynamic Light Scattering for biological macromolecules in solution

19 – 26 June 2016 | Suwon, Korea

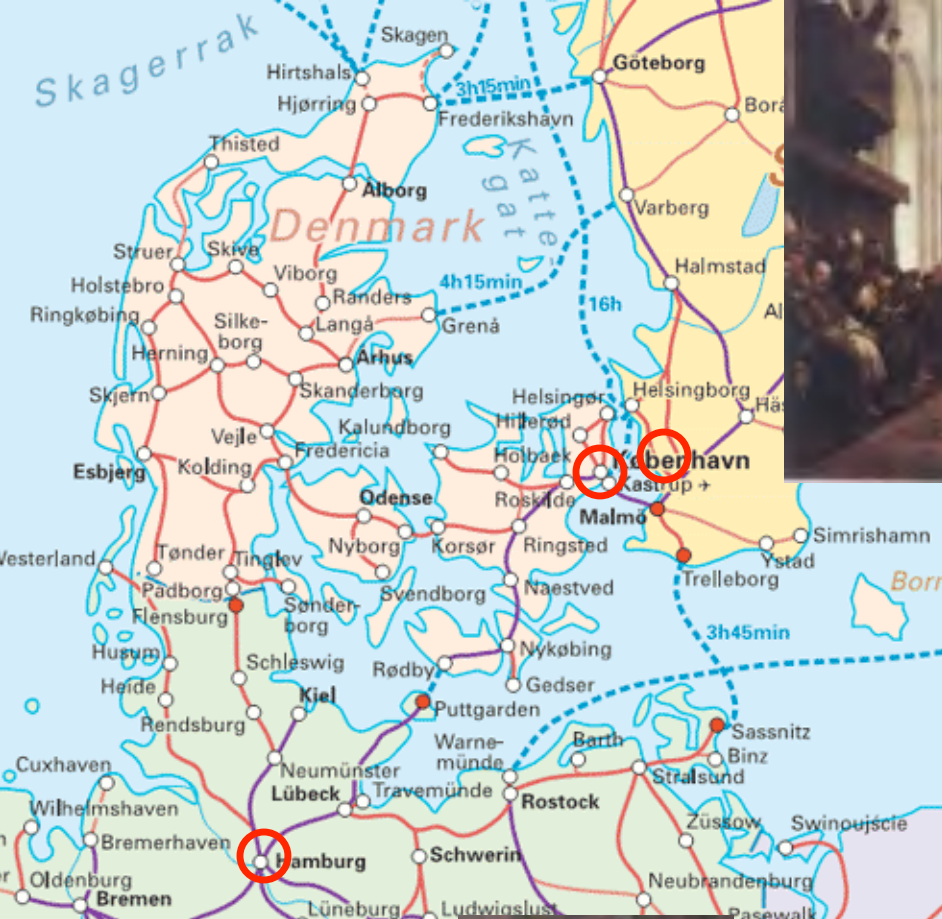
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University of Copenhagen

EMBO

**Global Exchange
Lecture Course**

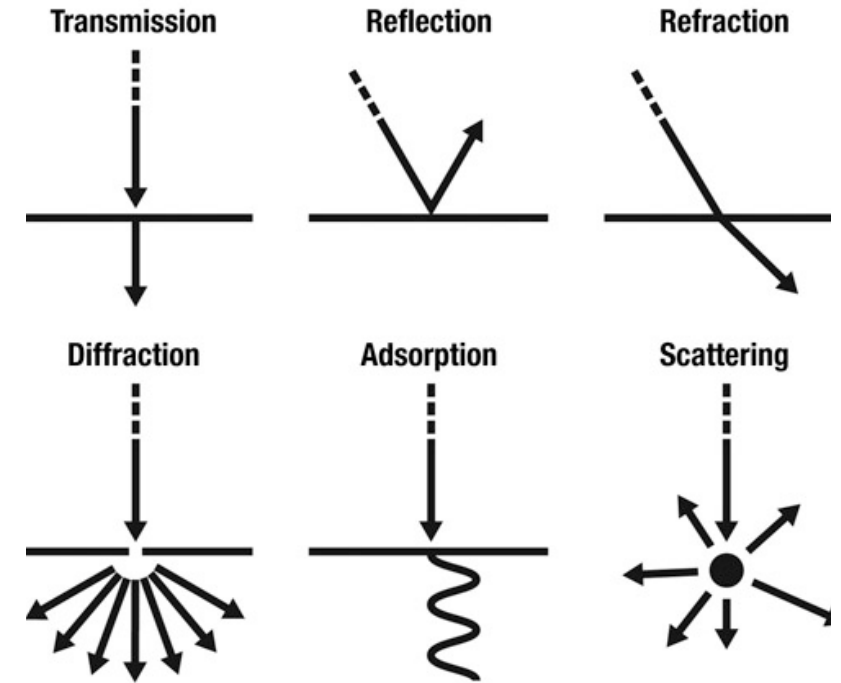




Positions opening in the fall 😊



When light interacts with matter, it can....



- Be absorbed
 - and re-emitted at modified λ (fluorescence)
- Change polarisation
- Be scattered
 - Reflected/refracted/diffracted from ordered matter
 - Inelastically (change of λ) e.g. Raman
- - all disregarded here

Rayleigh scattering: λ of light is significantly larger than the dimensions of the scattering particles (point scatterers)

- Be scattered
 - Elastic (same λ)
SLS
 - Quasi-elastic (nearly same λ)
DLS or QELS
 - movement of particles modifies λ (Doppler effect)

Why is light scattered?

Electrodynamics:

An oscillating dipole emits electromagnetic radiation in all directions

Induced dipole momentum (oscillating)

$$\mu = \alpha \cdot m \cdot E_{0,laser}$$

Polarizability

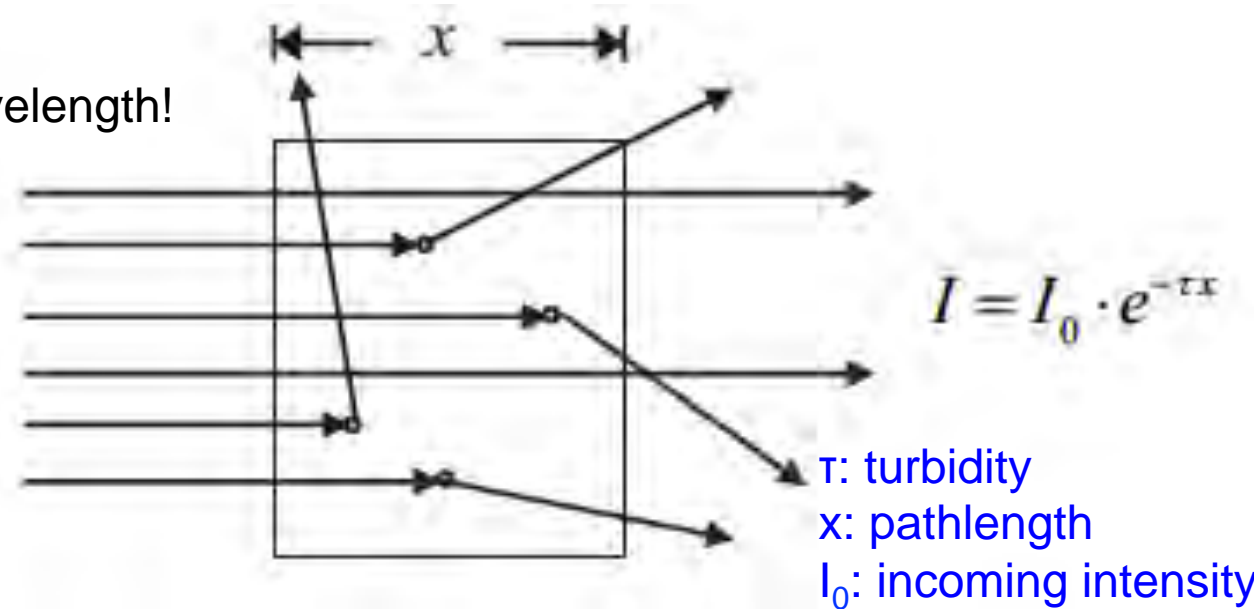
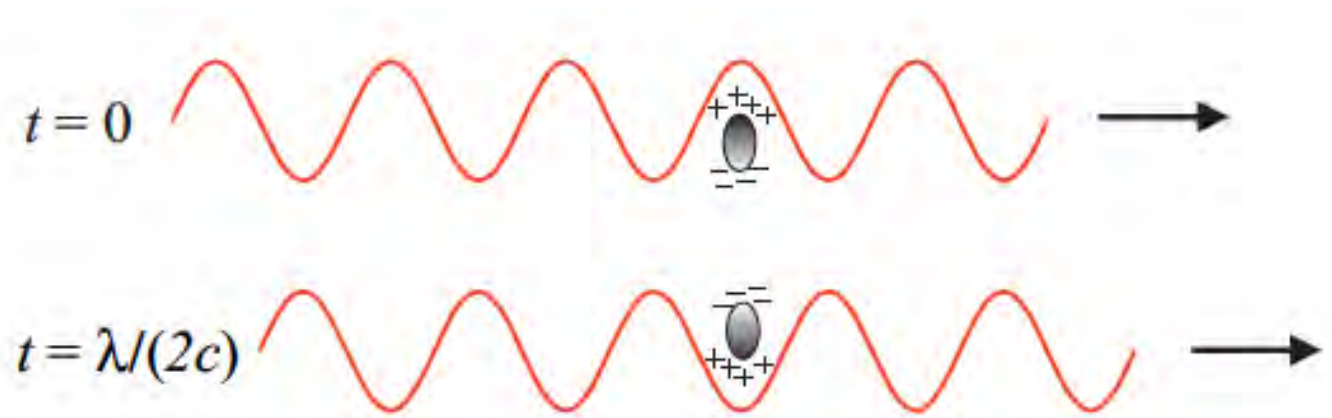
Mass of dipole

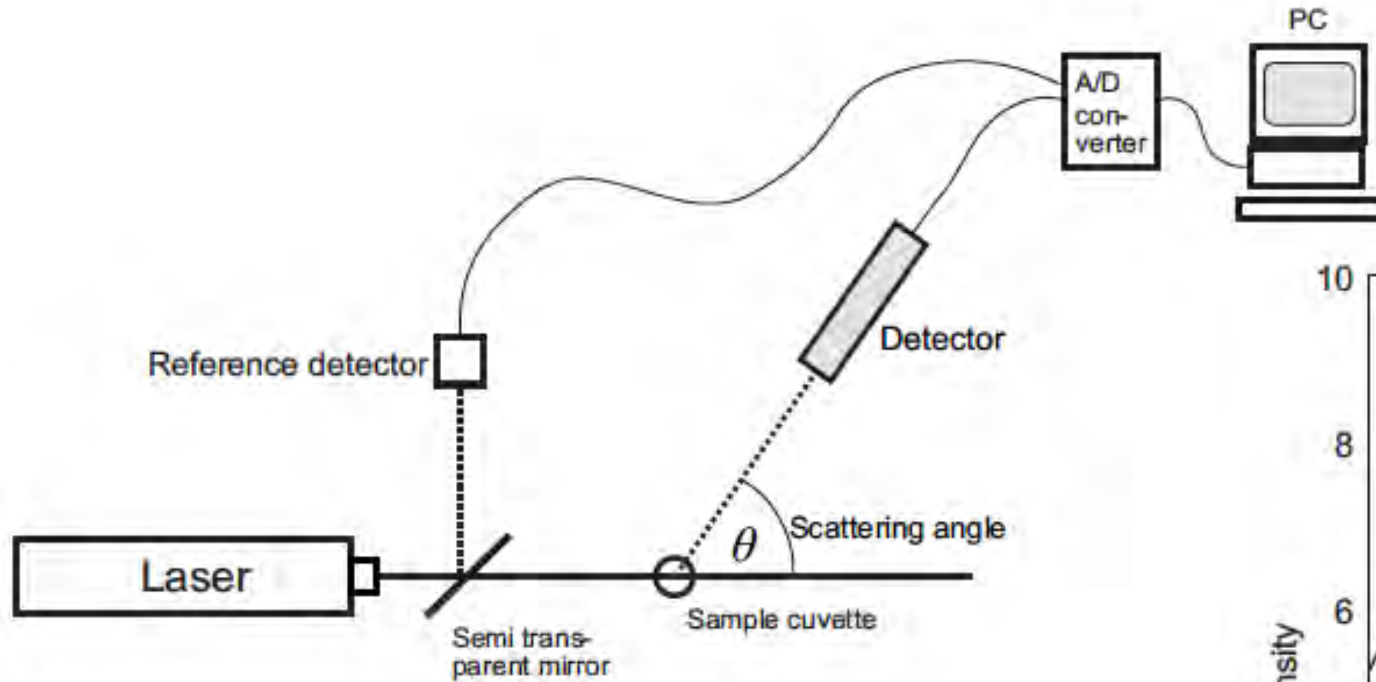
$$I_{s,1}(r) = I_0 \cdot \frac{\pi^2 \alpha^2}{r^2 \lambda^4}$$

Choose right wavelength!

The scattering intensity is proportional to the square of the particle molecular weight.

The scattered light is proportional to the concentration of the particle.

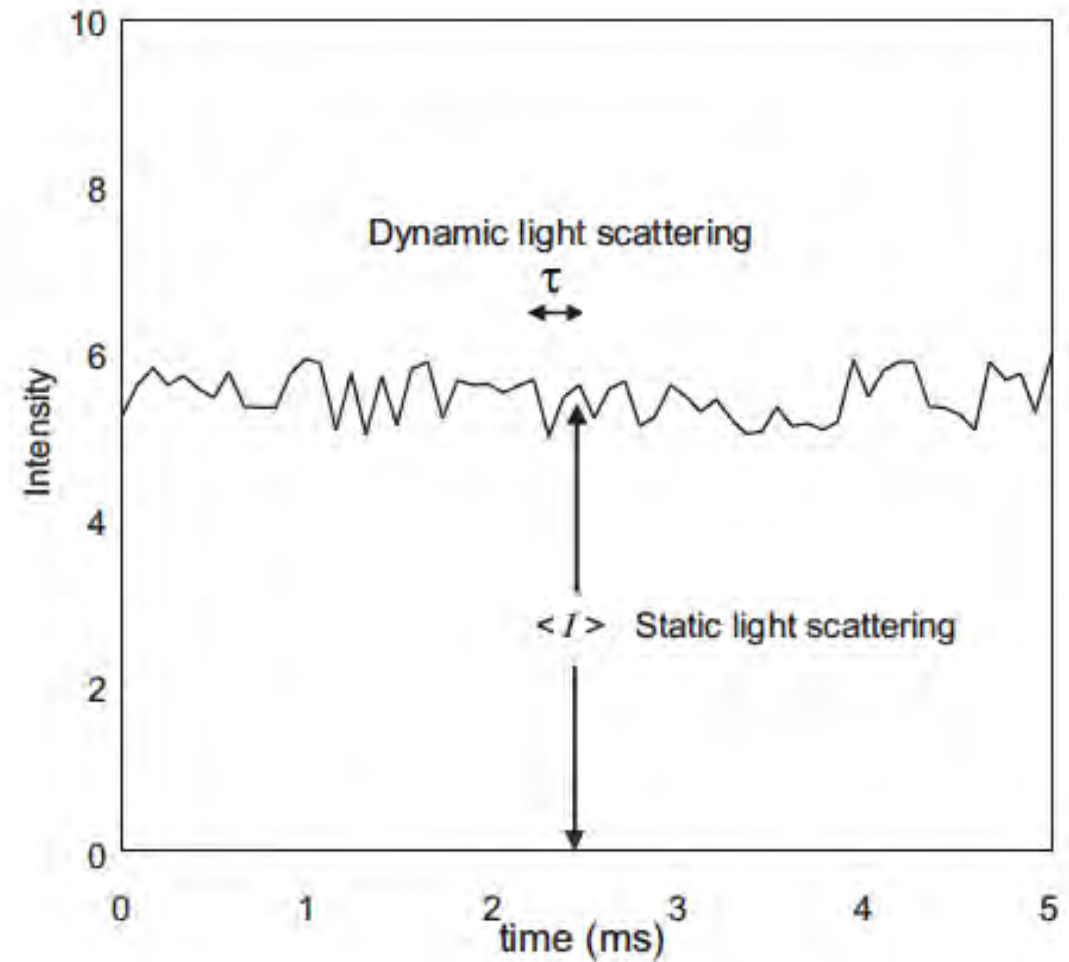




Monochromatic
Collimated

Intensity: Reflects the molecular weight of the particles

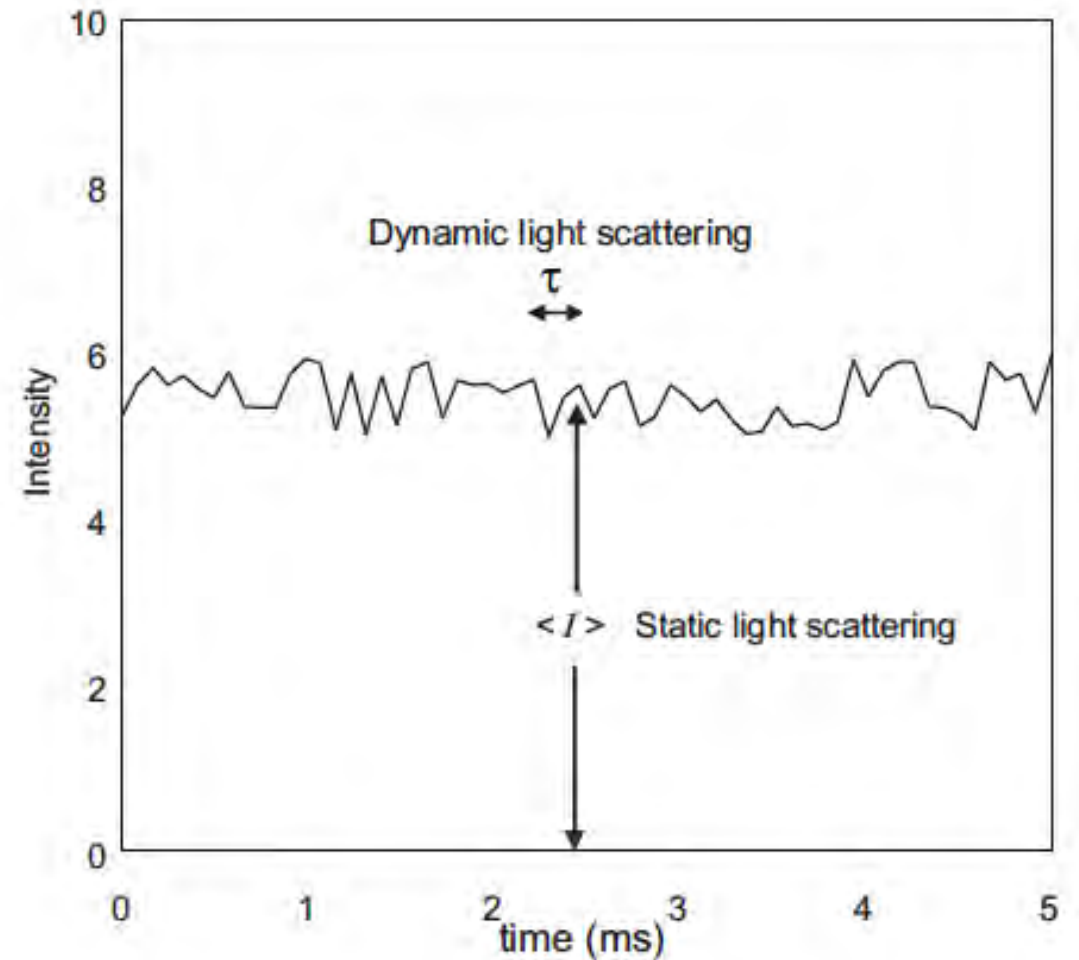
Fluctuations: Reflect the diffusion coefficient of the particles



Basics: SLS and DLS

Intensity: Reflects the molecular weight of the particles. SLS measures at many different angles (typically 10-100), intensity is averaged over time (1 sec or more)

Fluctuations: Reflect the diffusion coefficient of the particles. DLS employs measurements in a time series, averaging over very short time intervals (typically 100 nsec).



Basic comparison

- SAXS, SANS, SLS:
 - Same theory
 - Same experimental setup but different light sources
 - Measures the **structural characteristics** of the sample at different resolutions
 - Structure including both the form factor and structure factor
- DLS
 - Different theory
 - Different experimental setup
 - Measures the **diffusion** of the particles in the sample

Small Angle Scattering/Static light scattering

λ : Wavelength of X-ray, neutron or light

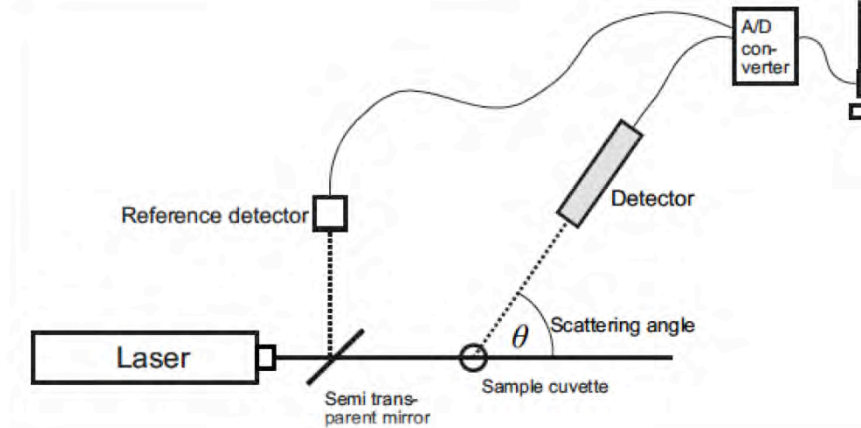
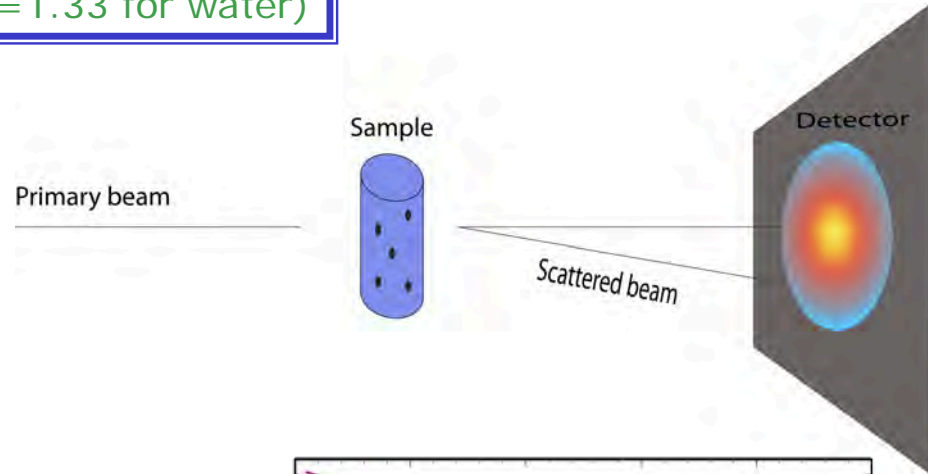
n_0 : Refractive index of sample (=1.33 for water)

Beam:

Neutron (SANS)

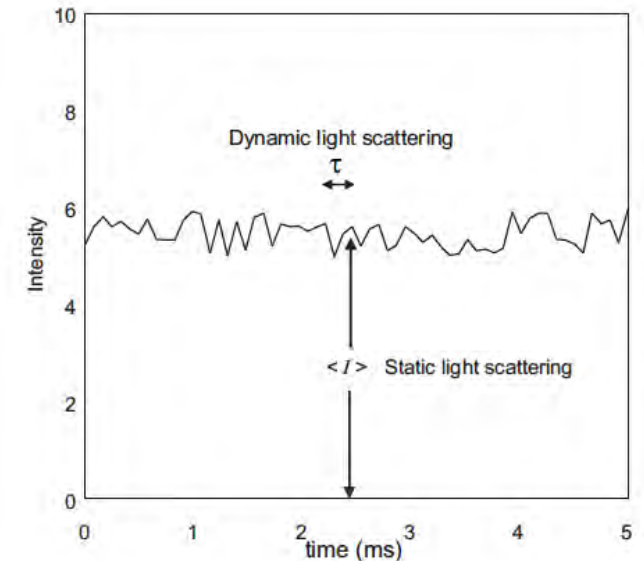
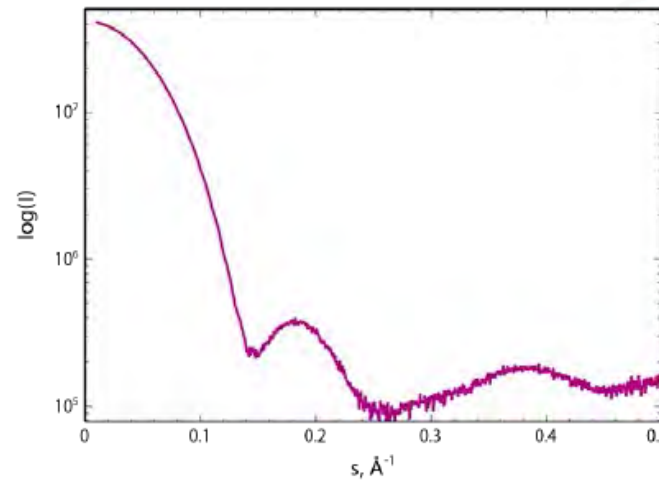
X-ray (SAXS)

or light (SLS)



$$|Q_{SAS}| = \frac{4\pi \sin \theta}{\lambda}$$

$$|Q_{SLS}| = \frac{4\pi n_0 \sin \theta}{\lambda}$$



SAXS/SANS: $\theta_{\min} \approx 0.03^\circ$, $\theta_{\max} \approx 3^\circ$, $Q = [0.001 - 0.5 \text{ 1/\AA}]$, 1-200 nm

SLS: $\theta_{\min} \approx 8^\circ$, $\theta_{\max} \approx 160^\circ$, $Q = [0.0004 - 0.001 \text{ 1/\AA}]$, 200-2000 nm

Static light scattering

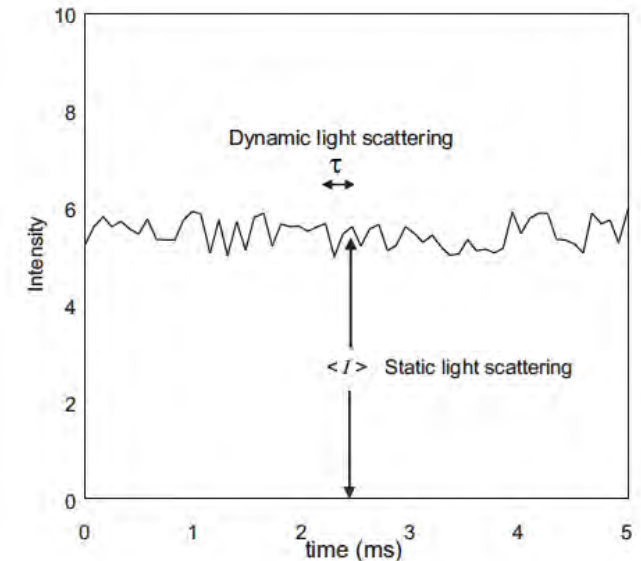
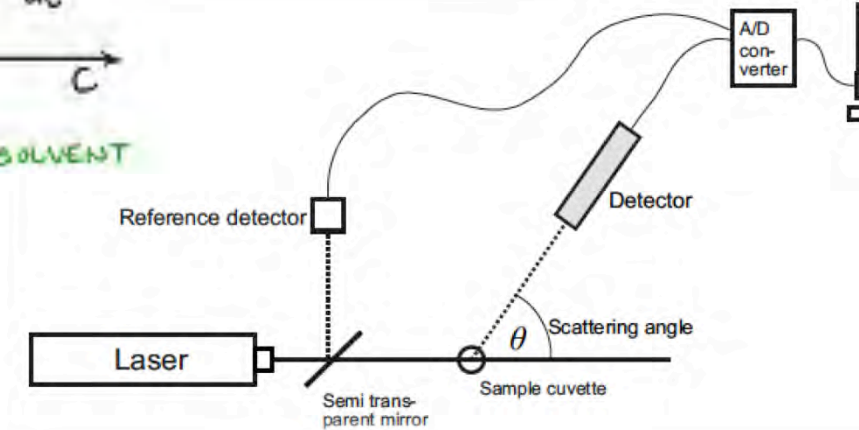
- Intensity depends on:
 - The molecular weight of the particles
 - The concentration of the particles
 - The size of the particles
 - The refractive index of the pure solvent
 - The refractive index of the suspended molecules
 - Interaction forces between particles

$$I_{\text{total}} = KI_0 VCM/r^2$$

C: mg/ml
 V: volume
 M: mass
 r: distance to detector
 K: optical contrast constant

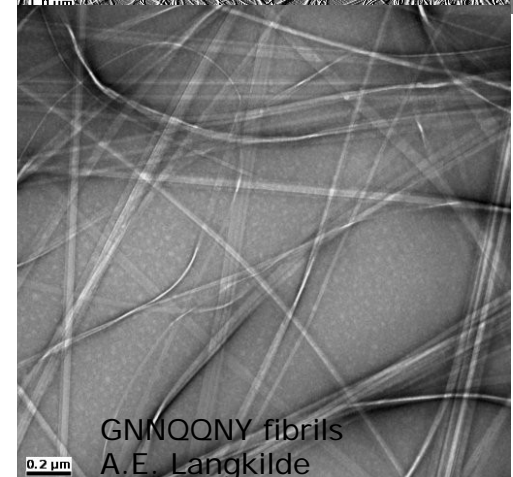
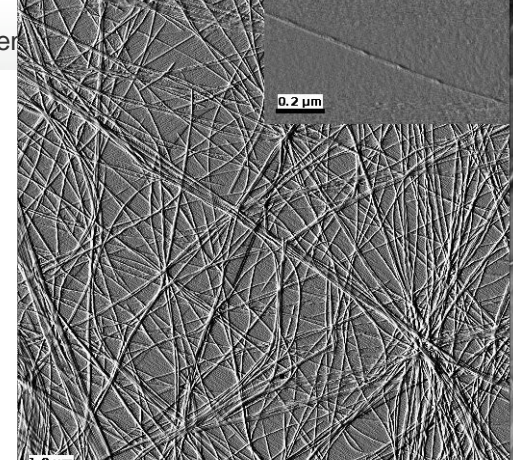
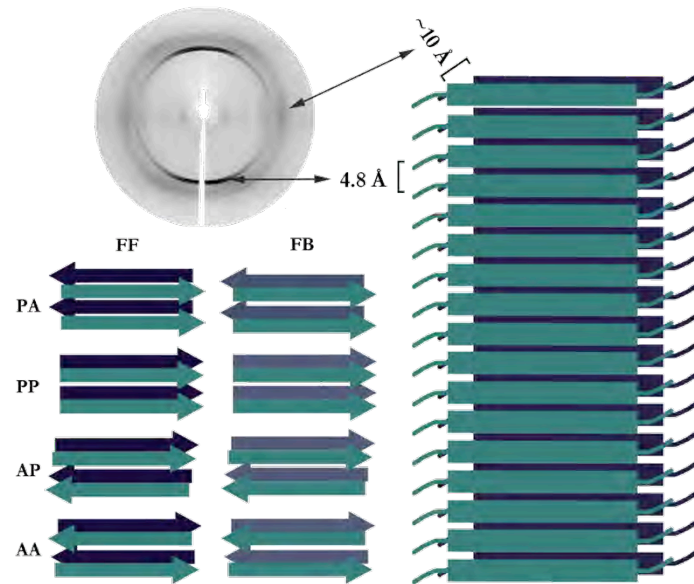


$$K = \frac{4\pi^2 n_0^2 (dn/dc)^2}{N_A \lambda_0^4}$$

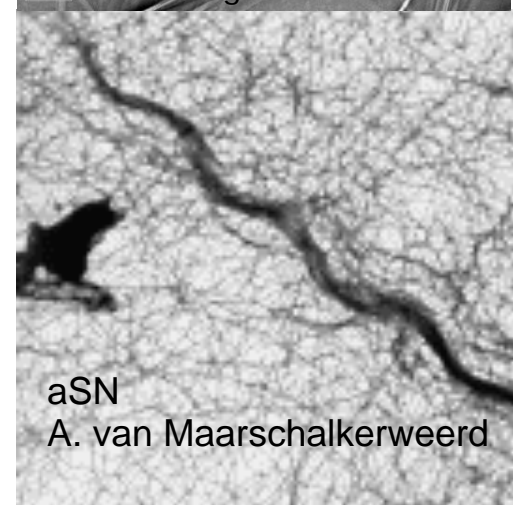


Amyloid(-like) fibrils

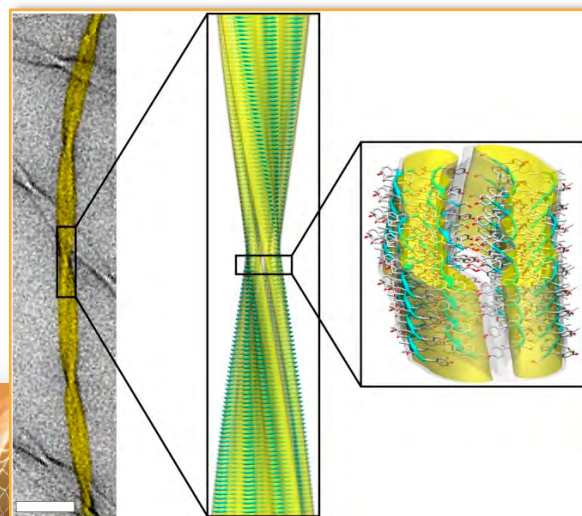
- Amyloid diseases (Alzheimers, Parkinsons...)
- Functional Fibrils (Antimicrobial, Biofilm, Spider silk)
- Biopharmaceutical stability (insulin, glucagon, ...)
- Self-assembly bio-systems
 - Drug delivery (Degarelix)
 - Nano-material: the strength of steel



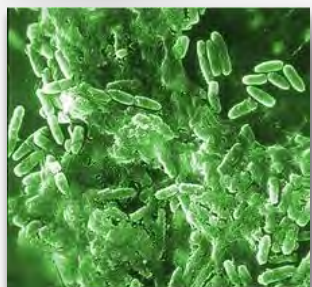
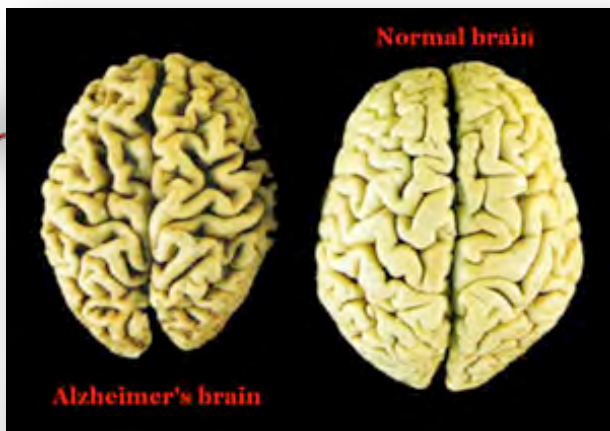
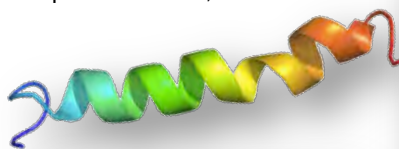
GNNQQNY fibrils
A.E. Langkilde



aSN
A. van Maarschalkerweerd



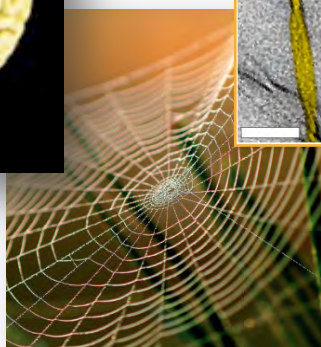
pdb-code 1d0r, GLP1



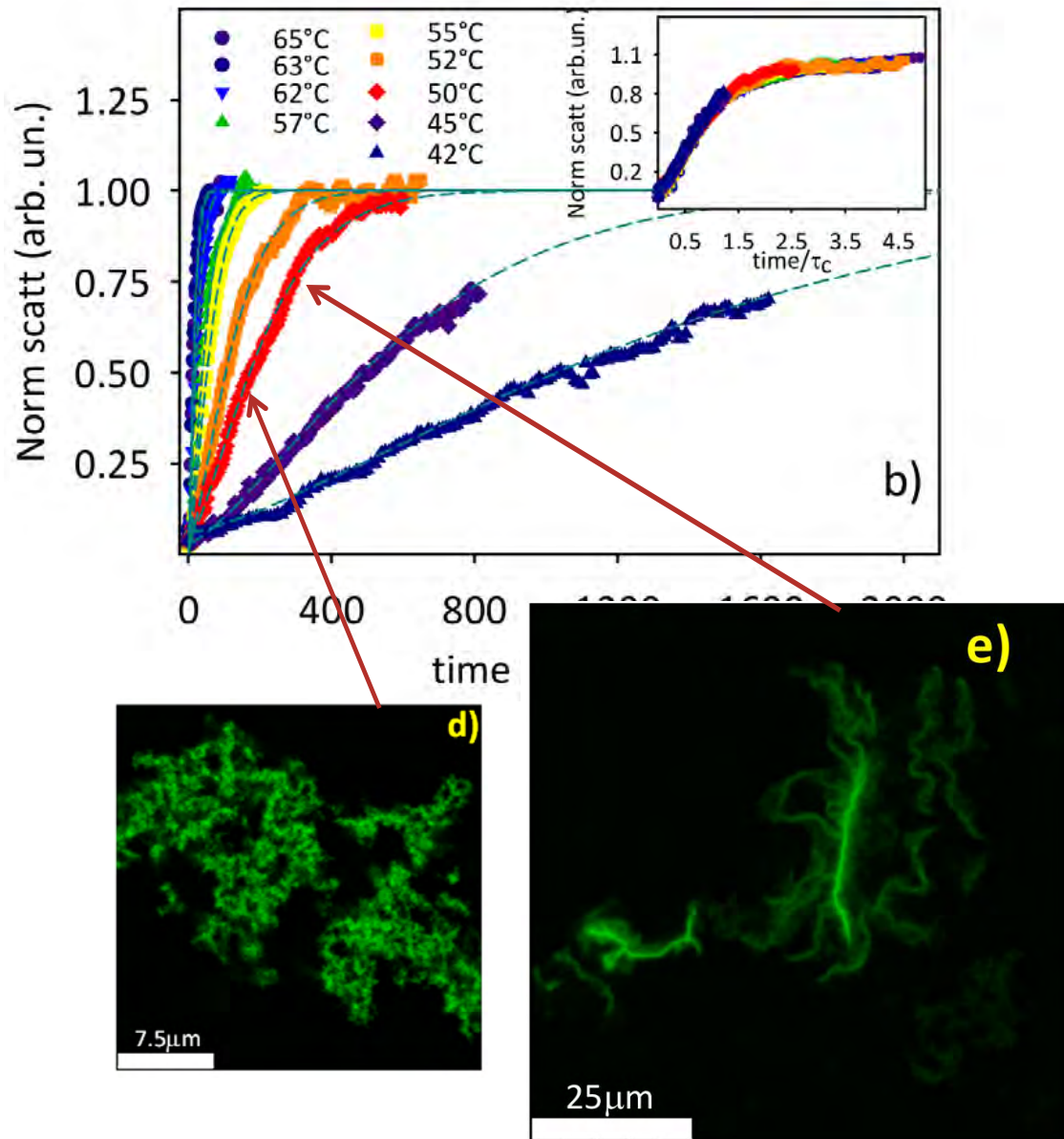
E. coli Biofilm AJC1/Flickr



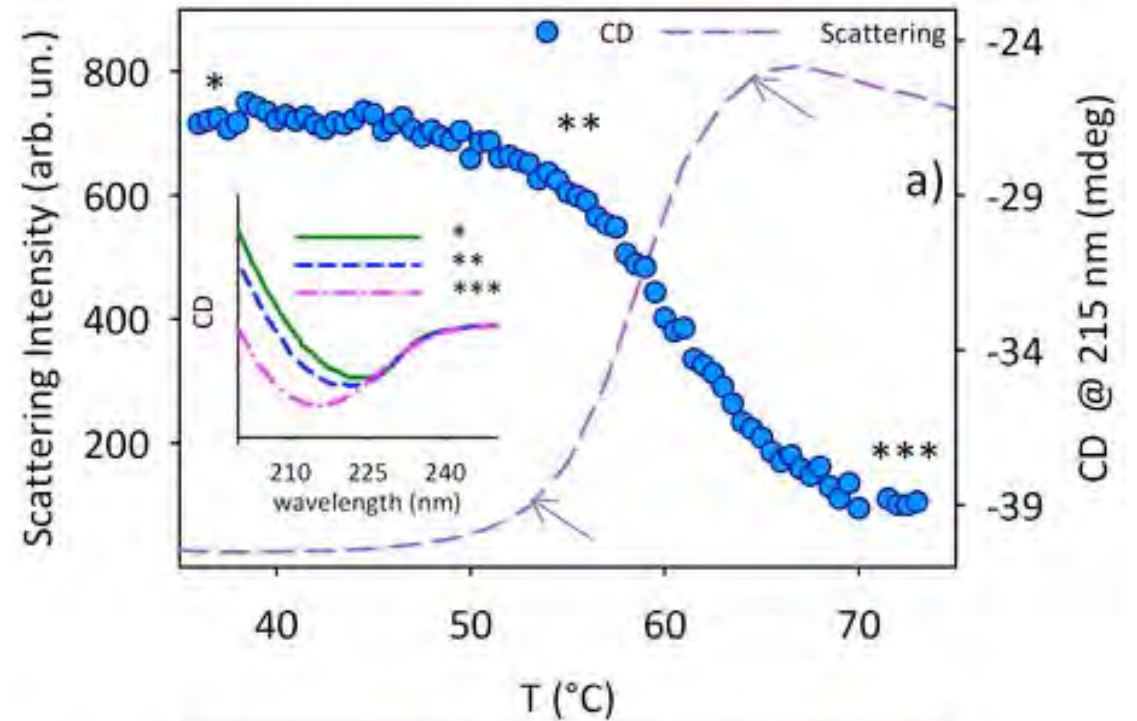
Am. Soc.Hematology



Applications: monitoring aggregate growth of ConA

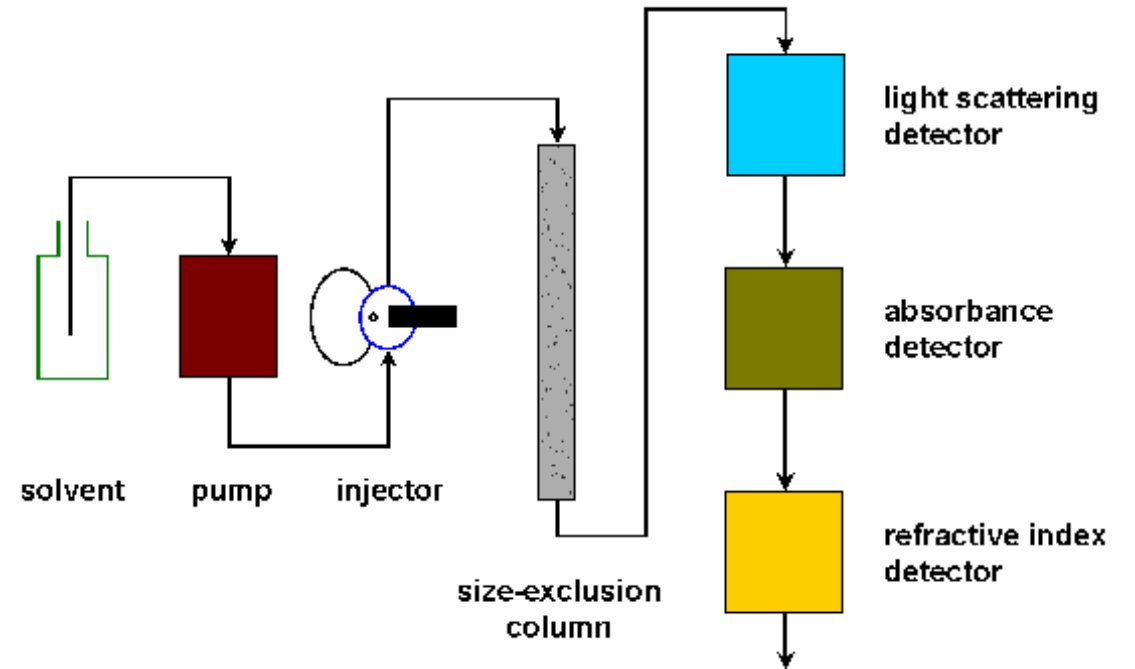


- Qualitative information
- Easy analysis
- Complemented with other techniques

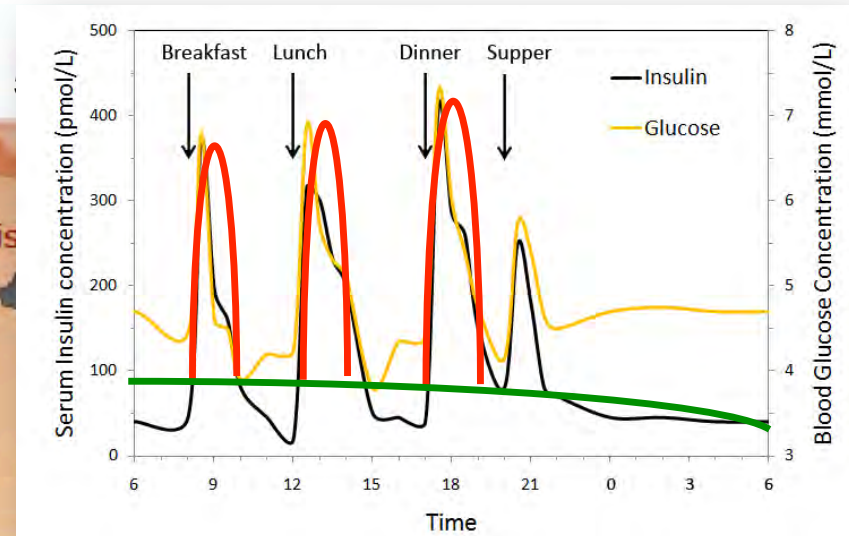
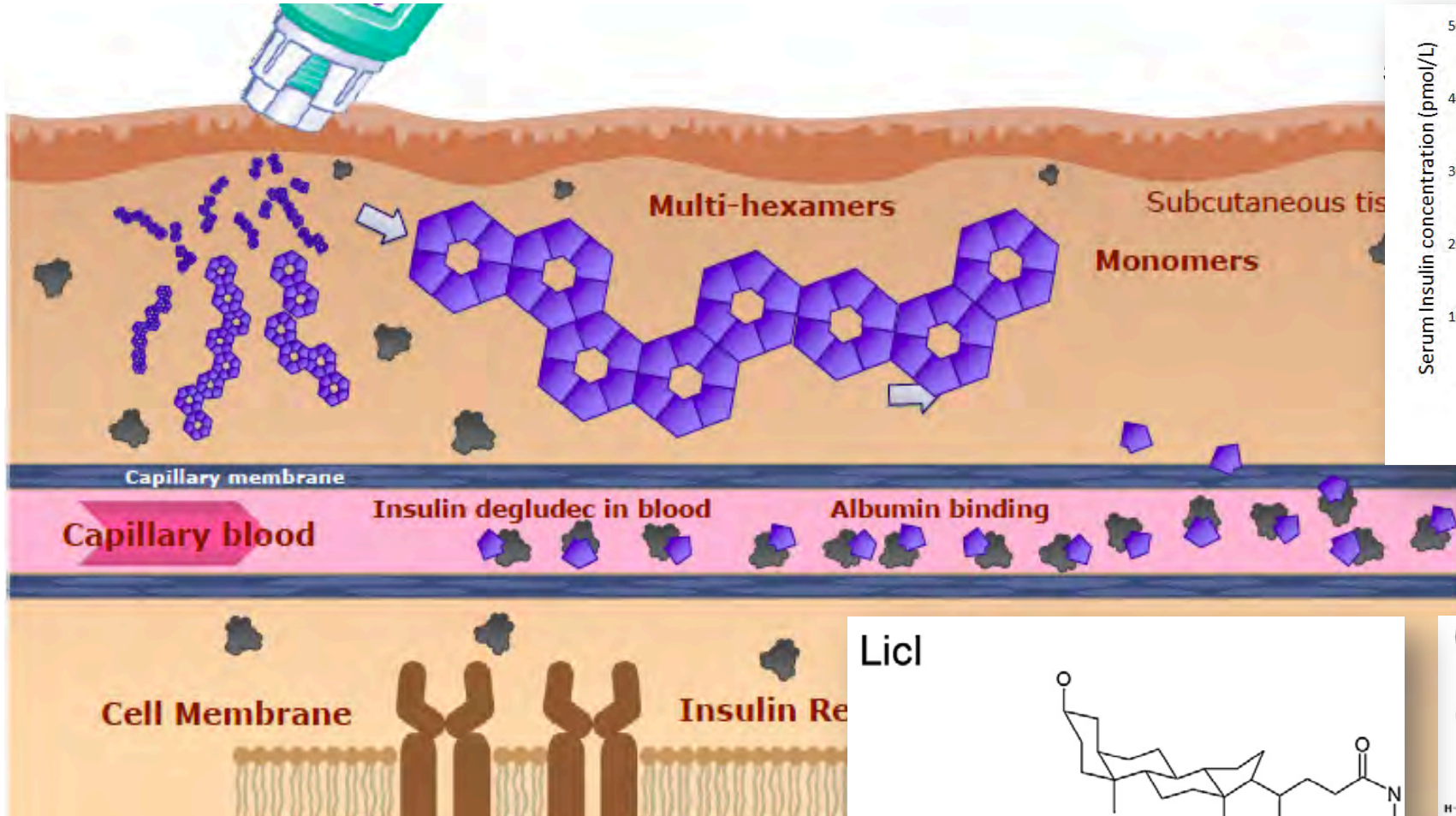


Coupling with Size Exclusion Chromatography

- Separate the molecular species according to size on a HPLC column
- Measure light scattering and derive molar mass on individual fractions
- Measure conc. of individual fractions via the refractive index



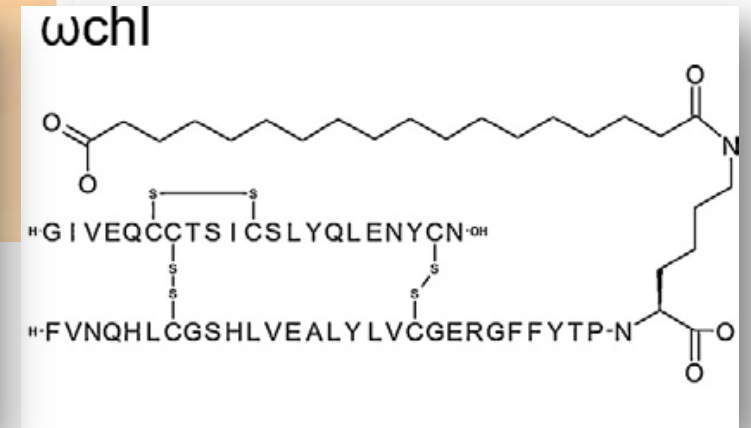
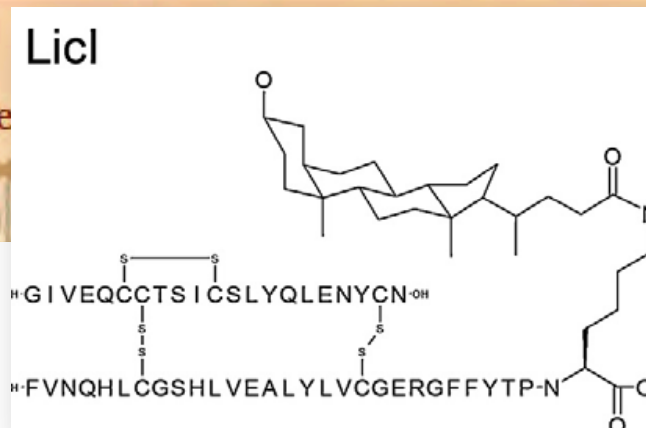
Therapeutically relevant insulin oligomerization



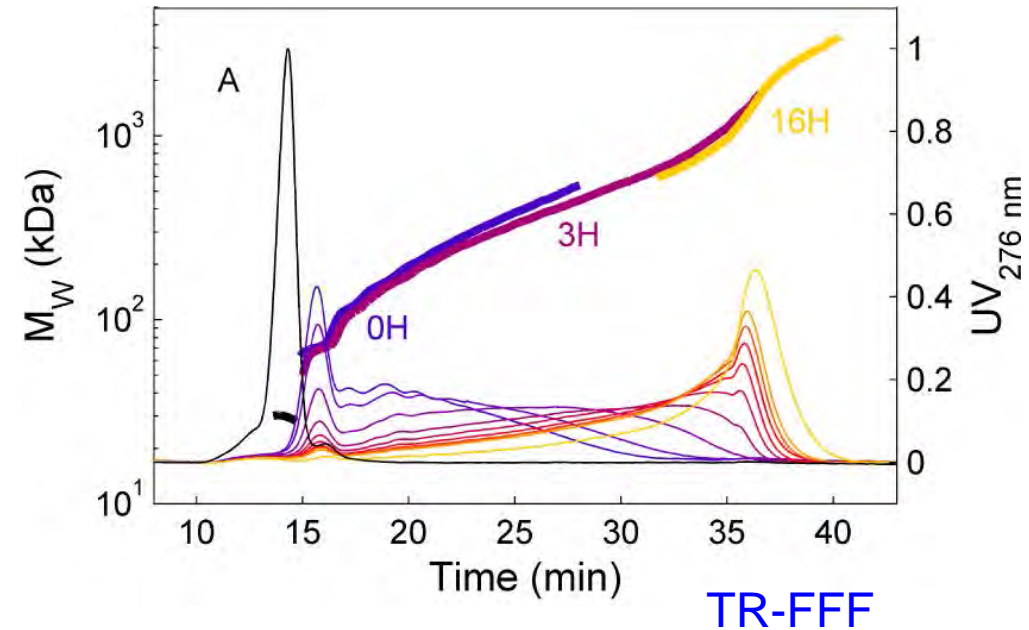
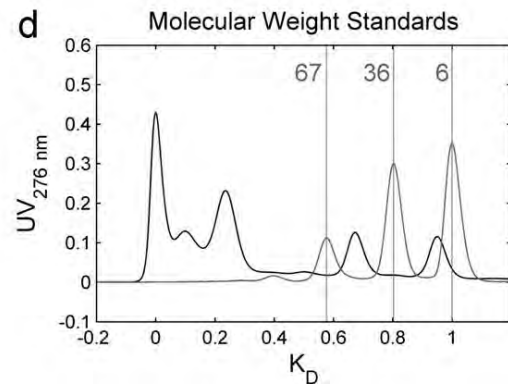
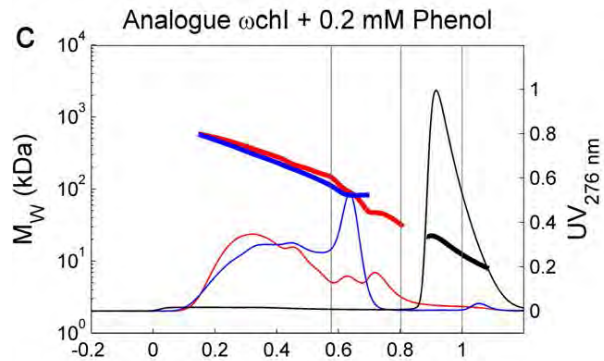
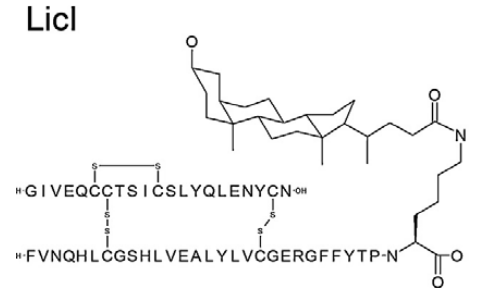
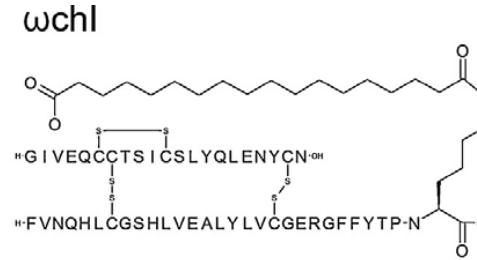
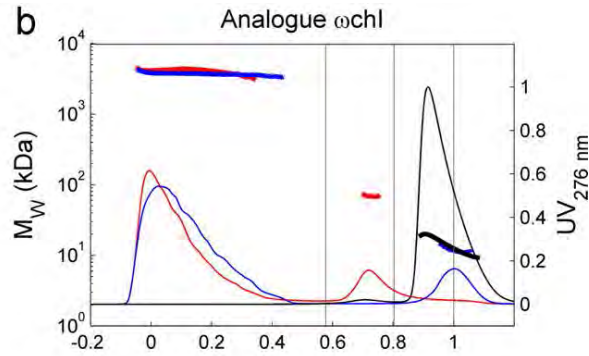
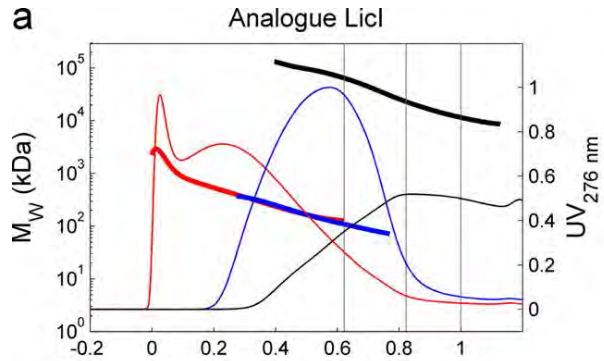
Fast acting insulin
Long acting insulin

Protein based drugs:

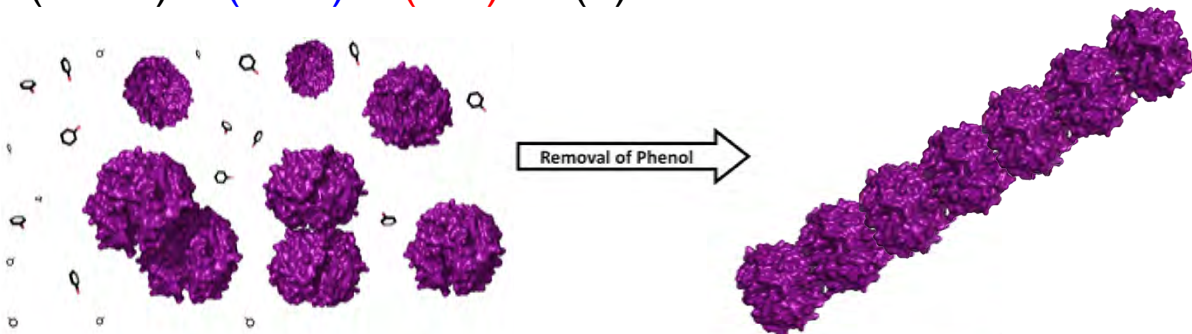
- Typically proteins in solution to be injected
- Control of release profile is desirable



Tuning experimental conditions by SEC-MALS



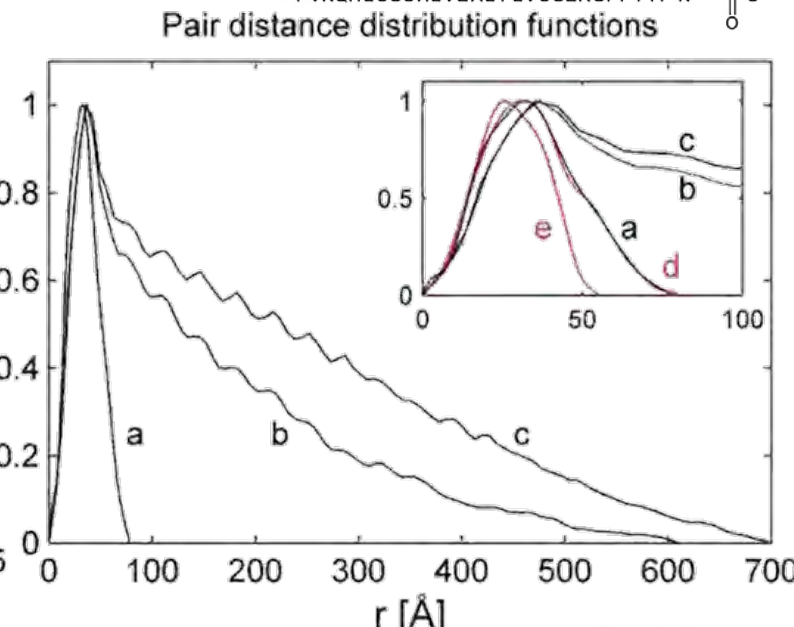
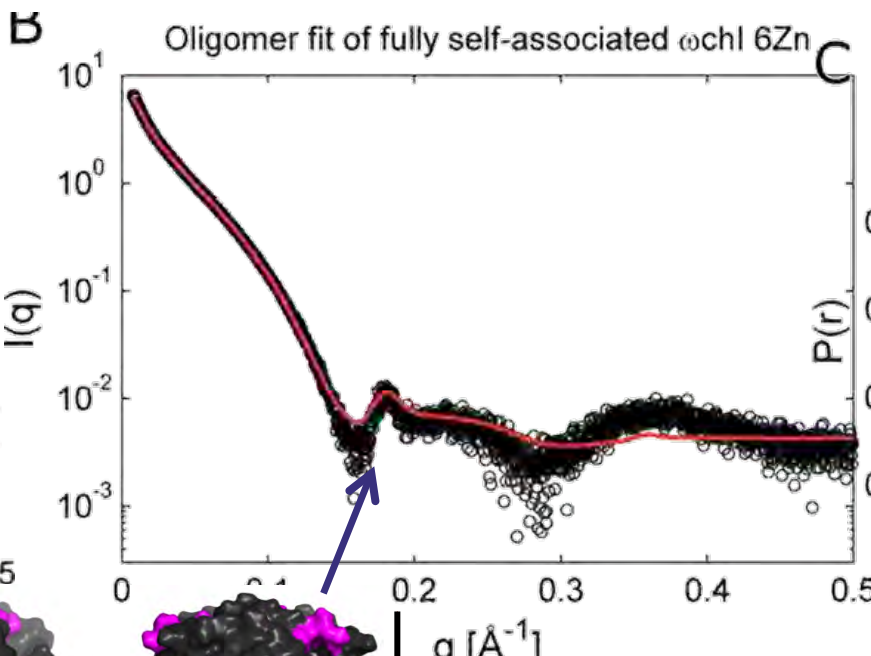
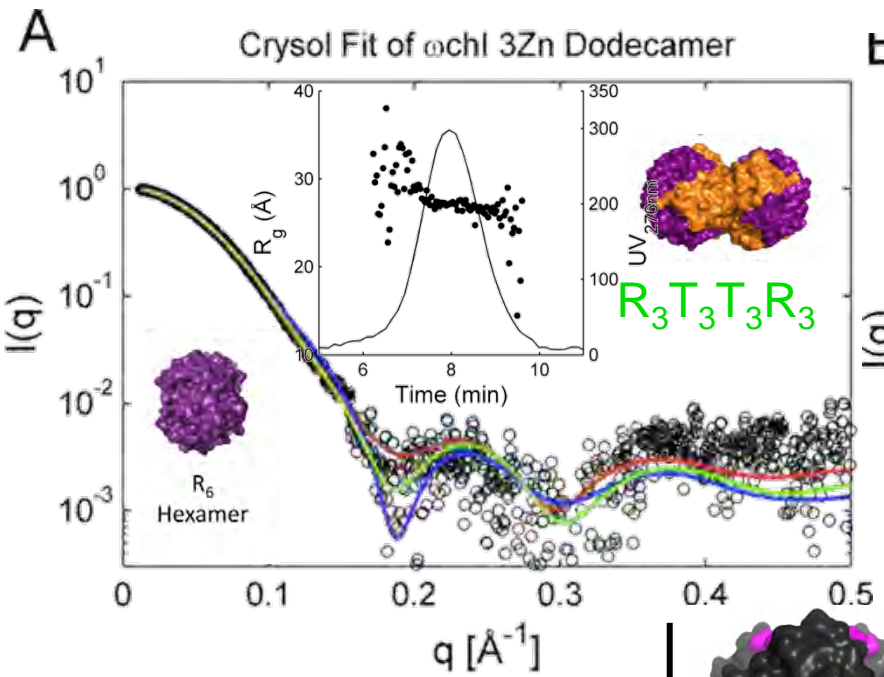
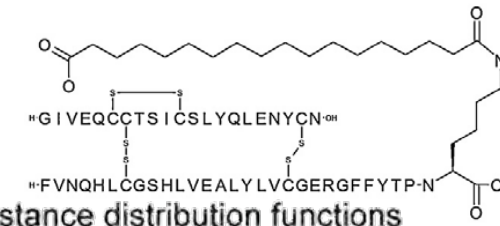
0 (black) 3 (blue) 6 (red) Zn(II)/6 Ins.



Jensen, M. H. et al (2011) J. Chrom. B;
Jensen, M.H. et al (2013) Biochemistry

Tuning experimental conditions by SEC-MALS

ω chl



$39.3 \pm 0.3 \text{ \AA}$

$33.9 \pm 0.2 \text{ \AA}$



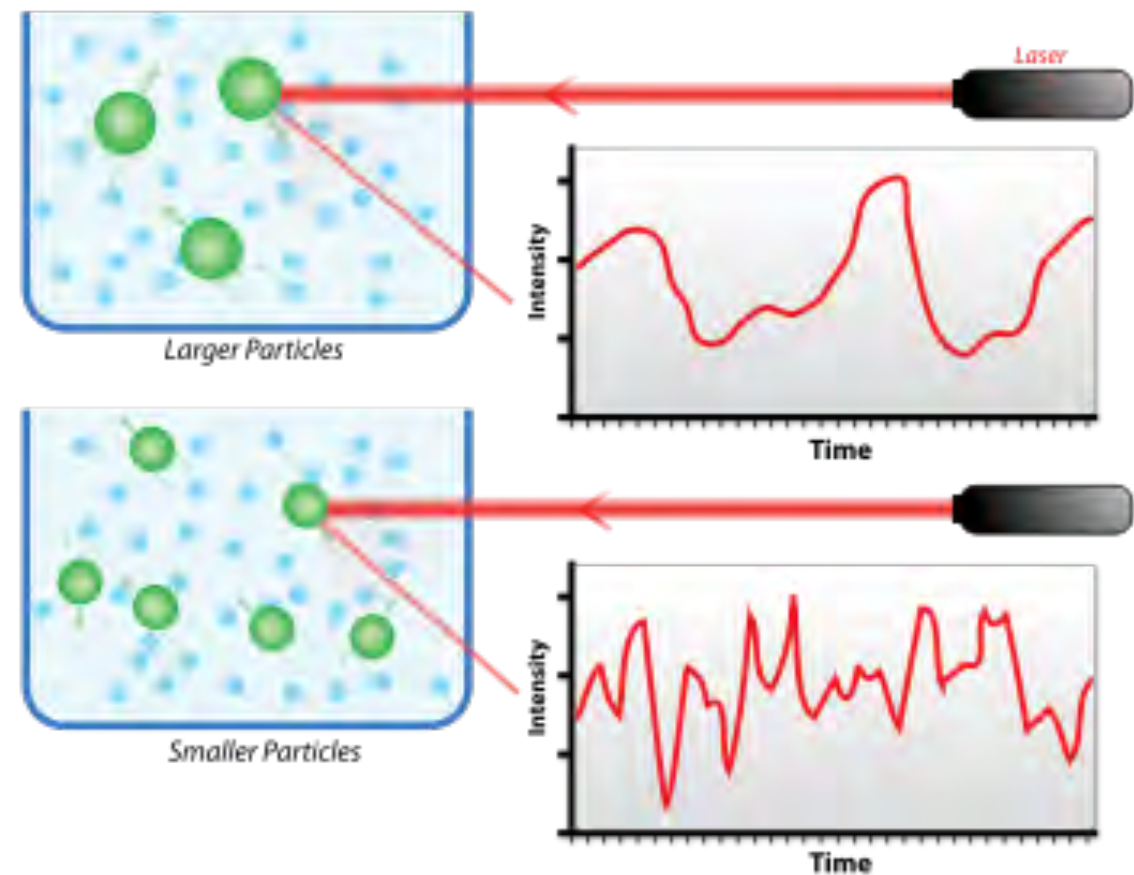
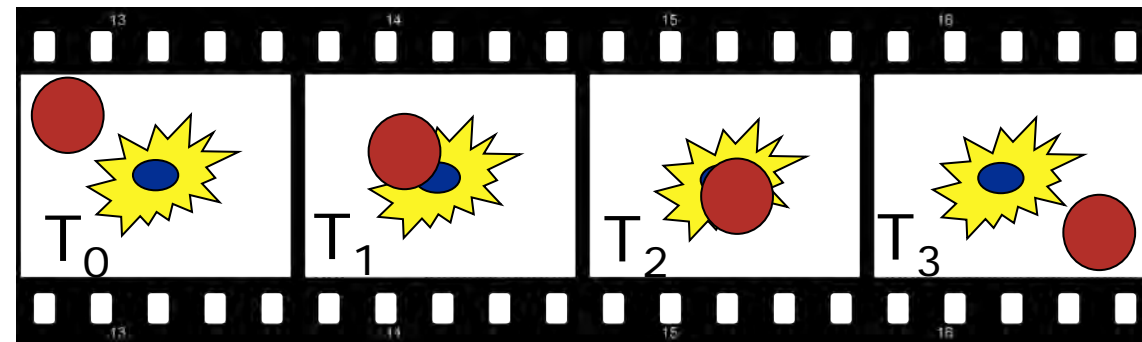
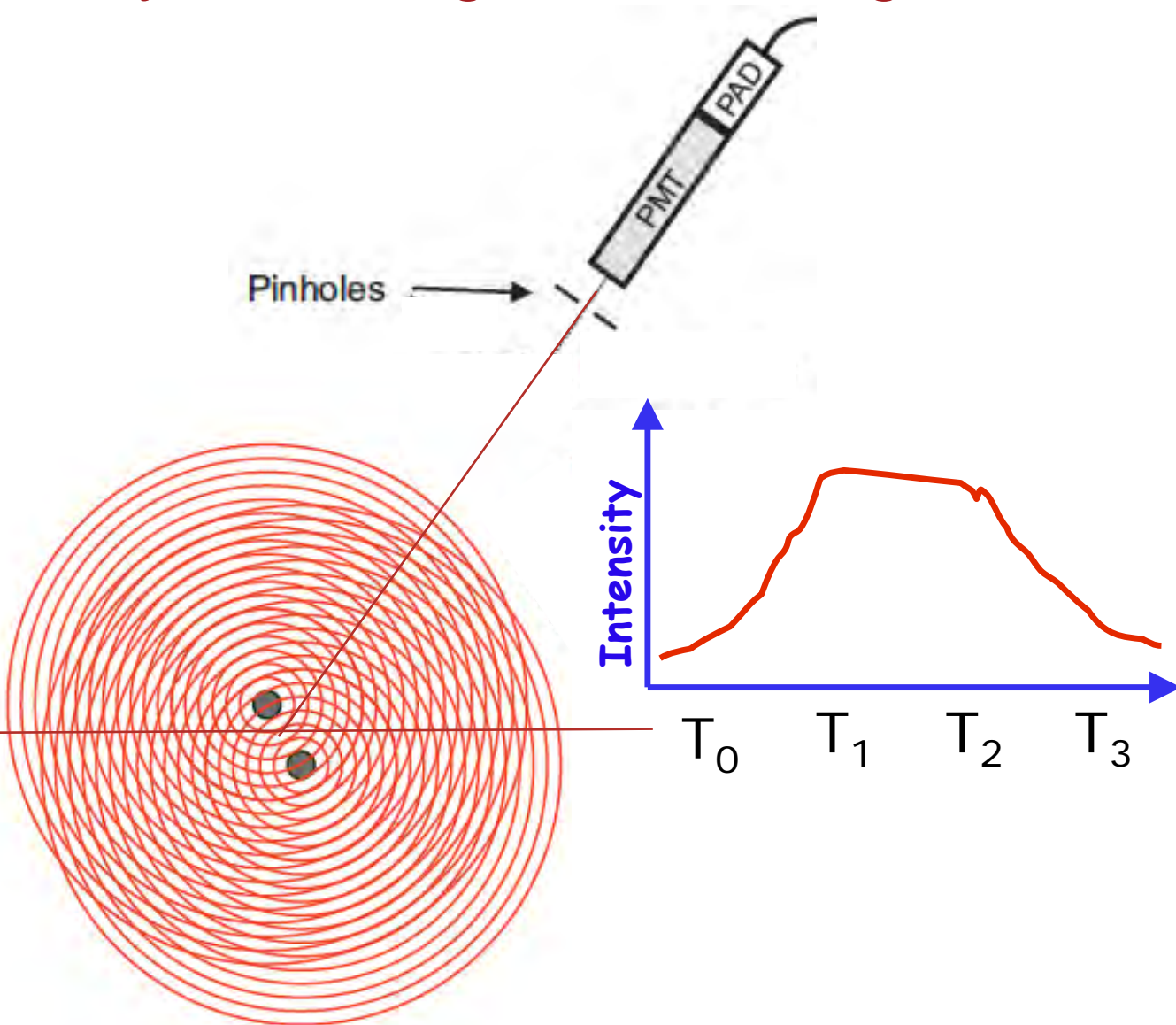
Jensen, M. H. et al (2011) J. Chrom. B;
 Jensen, M.H. et al (2013) Biochemistry

$R_3T_3T_3R_3$ Dihexamer

T_6T_6 Dihexamer

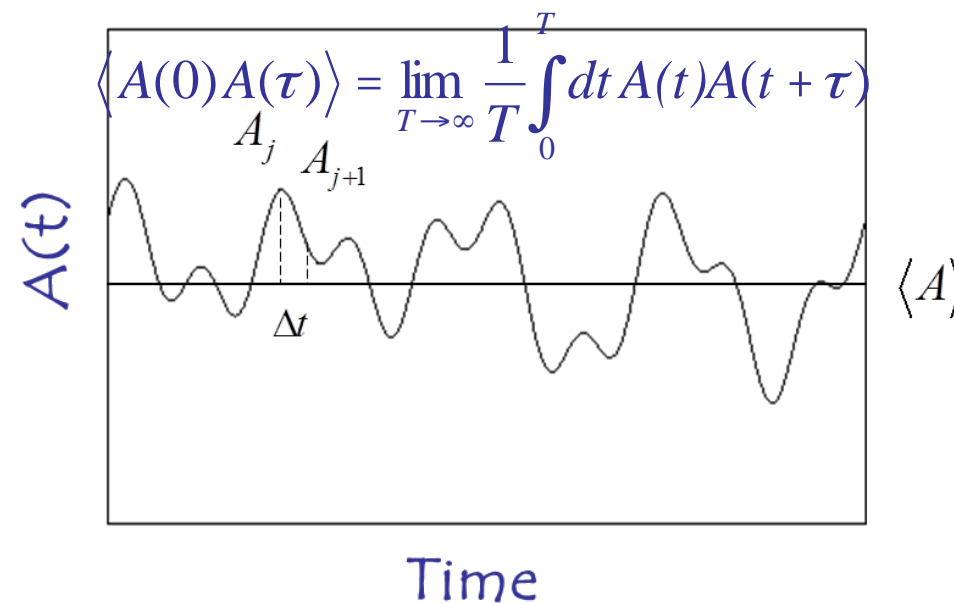
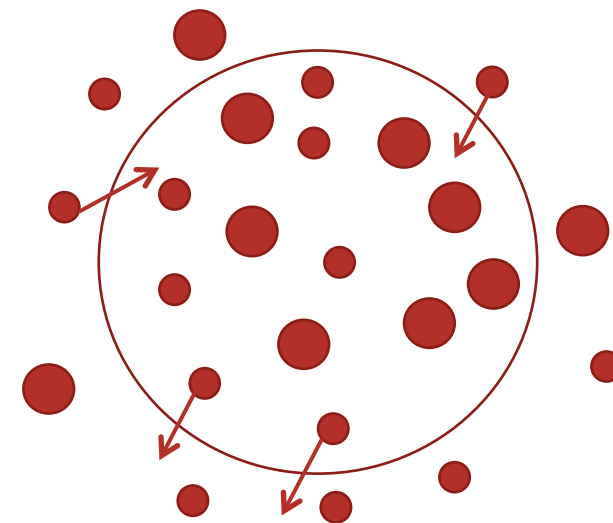
T_6 Multihexamer

Dynamic Light Scattering



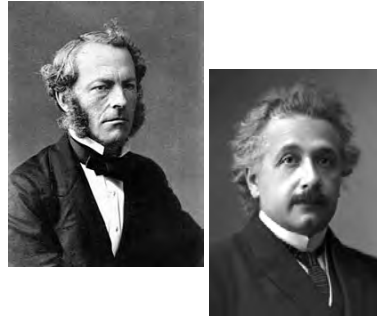
Dynamic light scattering – principle of measurement

- Fluctuations: Reflect the diffusion coefficient of the particles. DLS employs measurements in a time series, averaging over very short time intervals (typically 100 nsec).
- Frequency of fluctuations depends on how fast the particles move (large particles move slowly – small particles move faster ...)
- Amplitude of fluctuations depends on particle size, contrast, and concentration (for a given fixed λ)



The Stokes-Einstein relation for spherical particles:

$$D = \frac{k_B T}{6\pi\eta r}$$



T: absolute temperature
 k_B: Boltzmann's constant
 η: Viscosity of liquid

$$r_h = \frac{k_B T}{6\pi\eta D_{meas.}}$$

The hydrodynamic radius

Measure of the diffusion coefficient *D*

Then calculate equivalent hydrodynamic radius:

Range: Down to $r_h \sim 1$ nm
 Up to $r_h \sim 1000$ nm

The characteristic decay time

Diffusion in one dimension:

$$\langle x^2 \rangle = 2D \cdot t$$

D: Diffusion coefficient

t: time

x: displacement

$$x = \frac{1}{q}$$

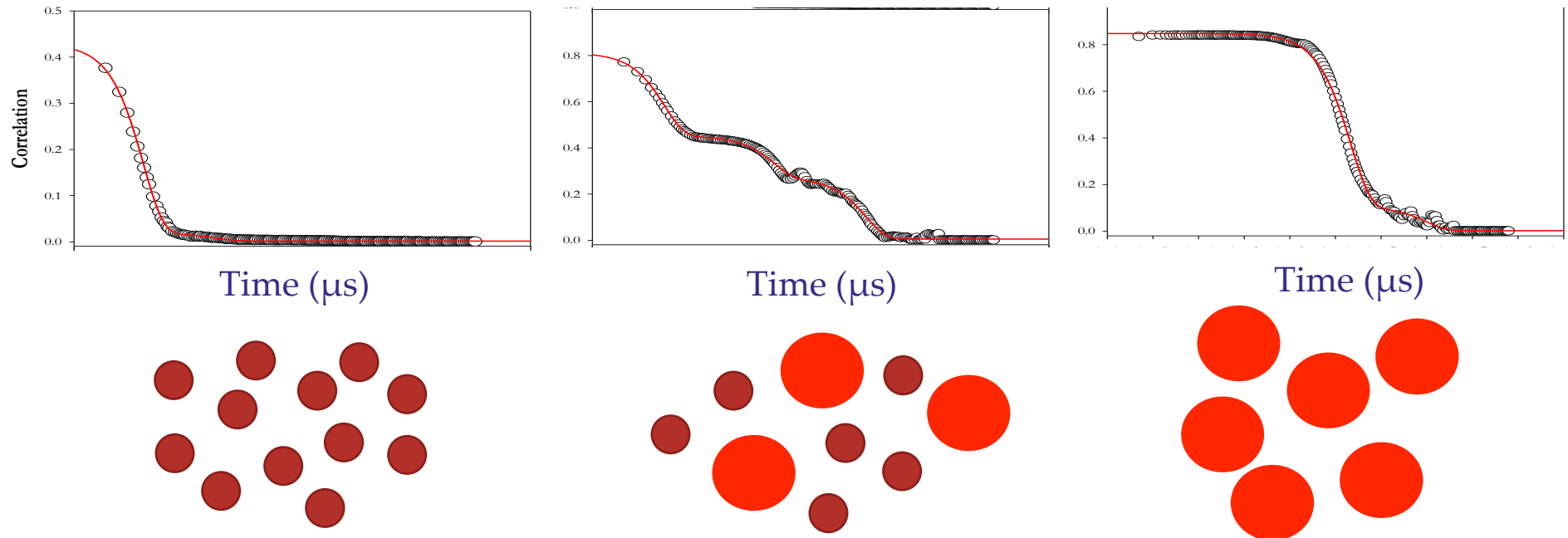
Characteristic diffusion distance for change in interference:

$$\left(\frac{1}{q}\right)^2 = 2D\tau_0 \Rightarrow \tau_0 = \frac{1}{2Dq^2}$$

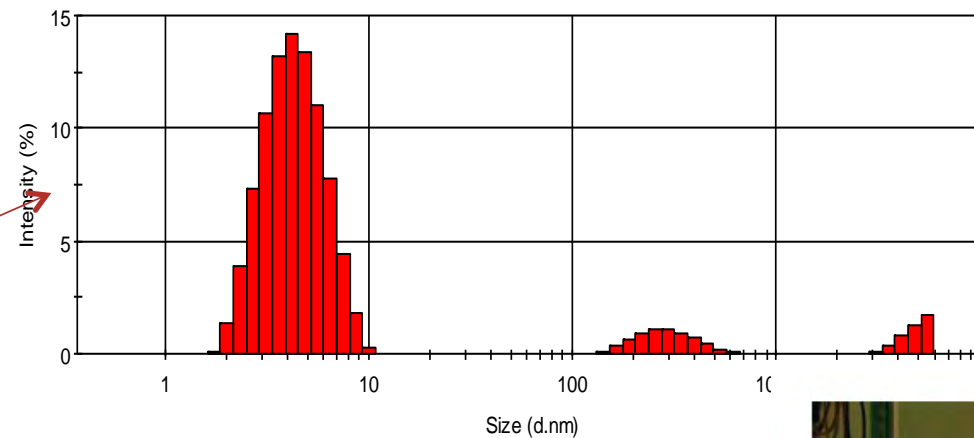
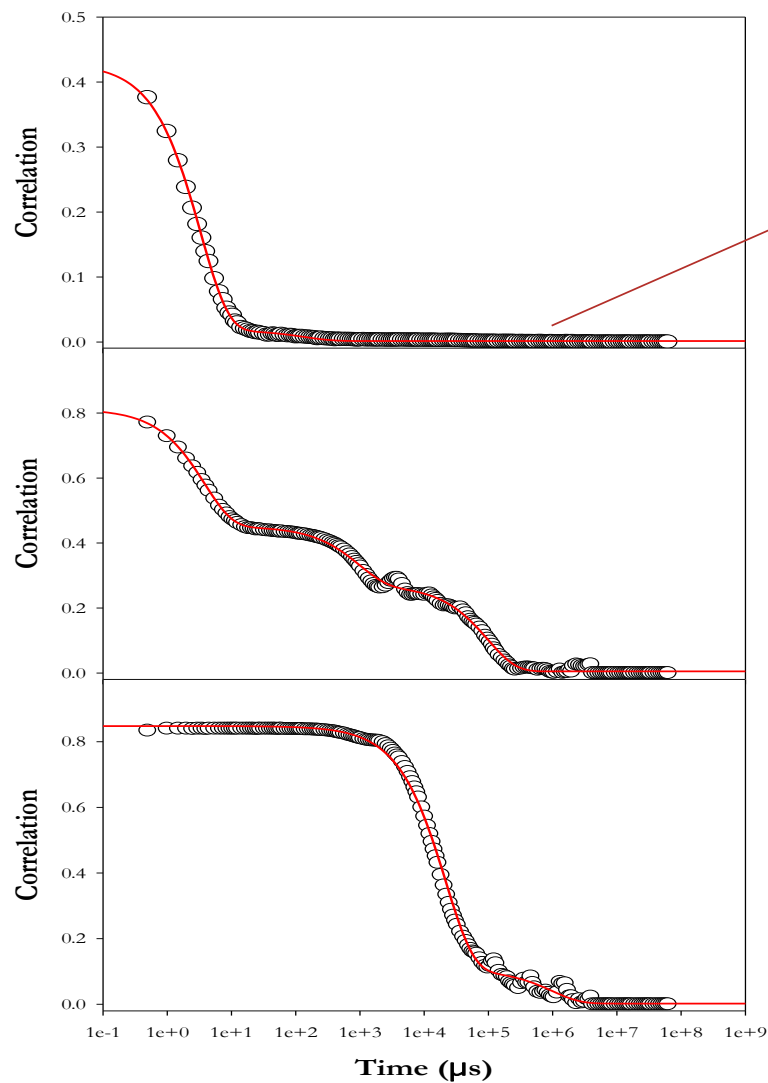
Dynamic light scattering – principle of measurement

$$G_2(\vec{q}, t) = \frac{\langle |A(\vec{q}, t)| |A(\vec{q}, t + \tau)| \rangle}{\langle |A(\vec{q}, t)| \rangle^2} = \langle N \rangle^2 + \langle N \rangle^2 e^{-2Dq^2\tau}$$

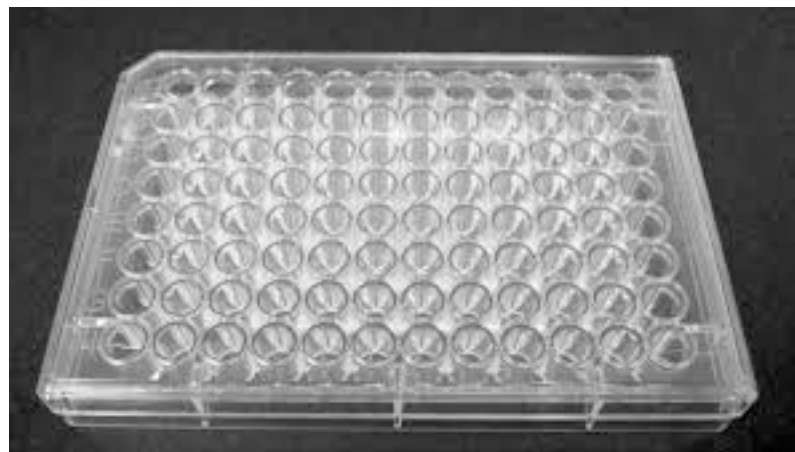
The Auto-correlation function: Cross-correlation of a signal with itself over time (similarity as a function of the time-lag between signals)



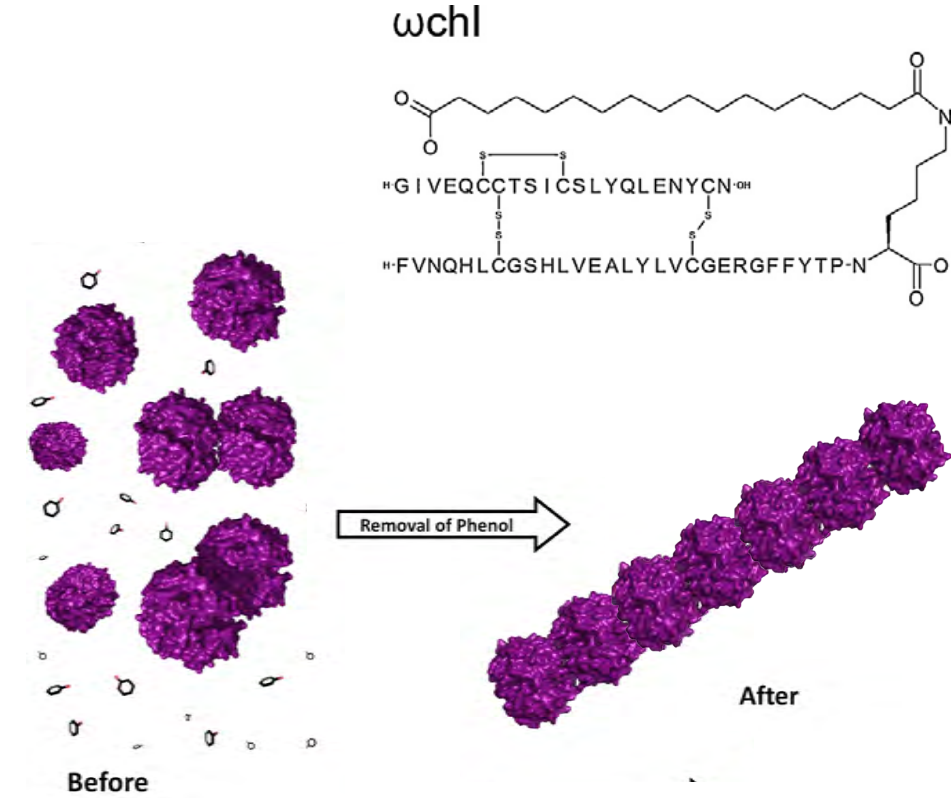
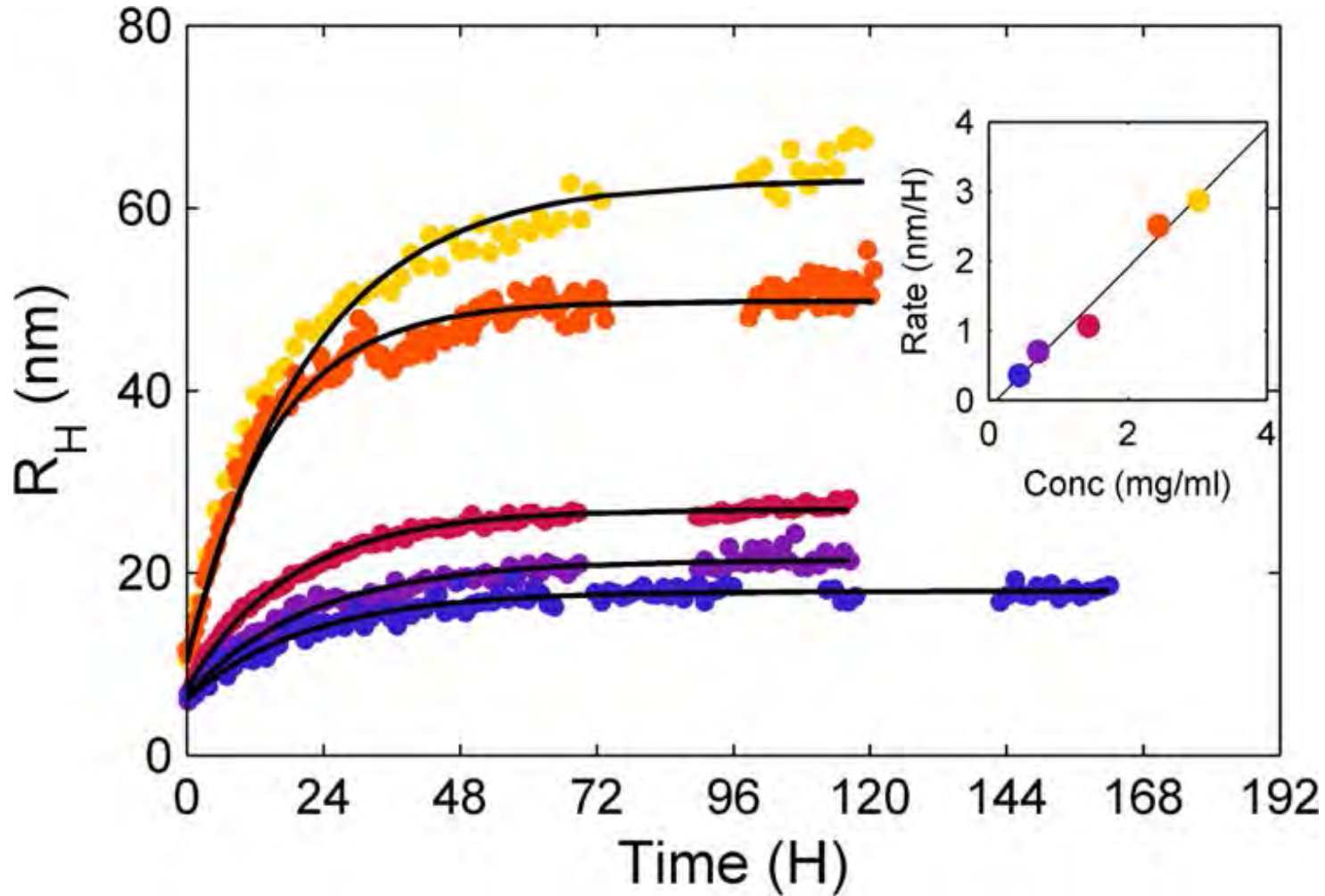
Size distribution for macromolecules in solution



- Quantitative information
- Easy analysis (if the software automatically does it)

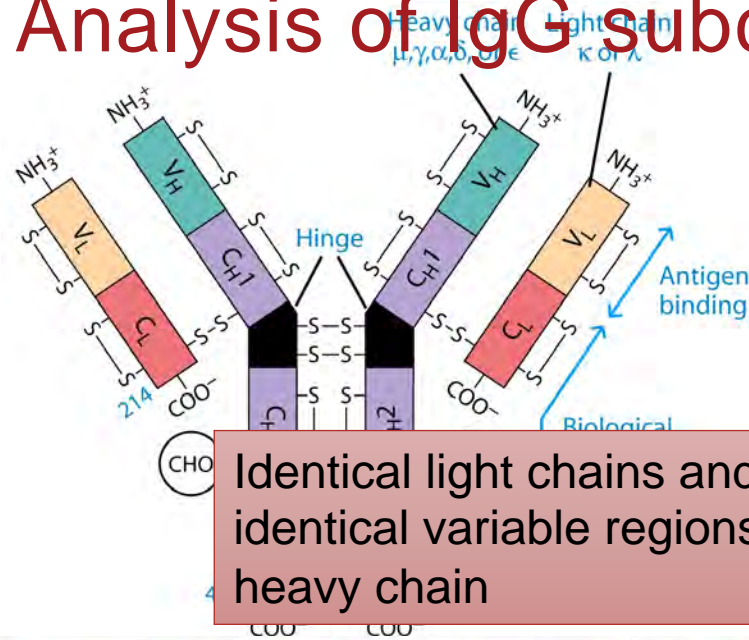


Back to the growing oligomers of insulin analogues

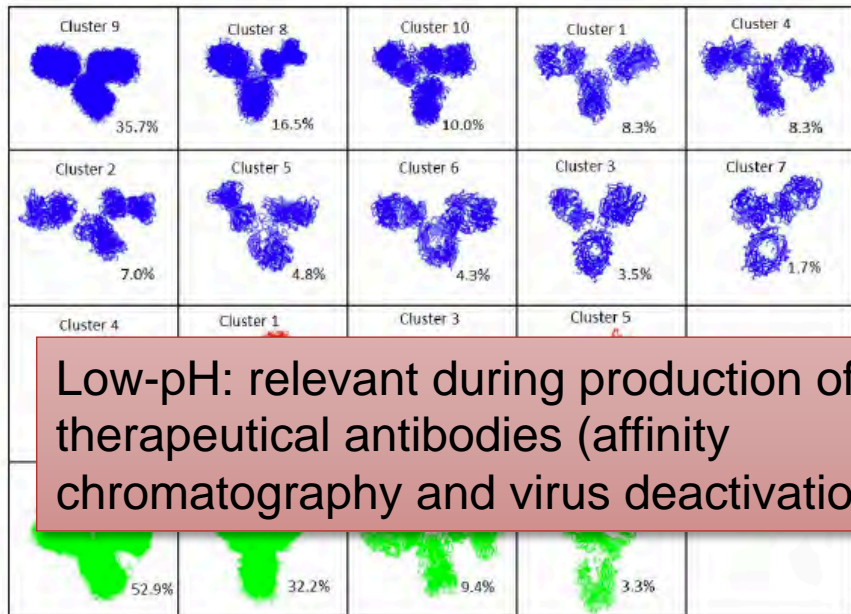


Note complementarity and advantages with DLS versus SLS?

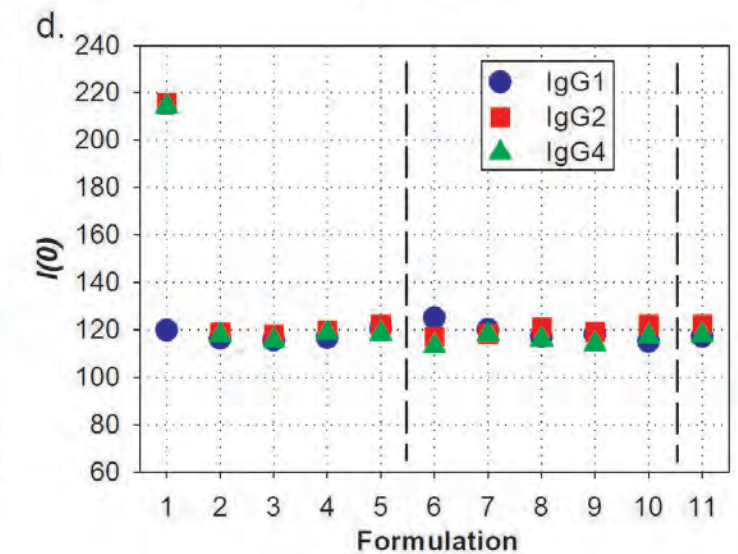
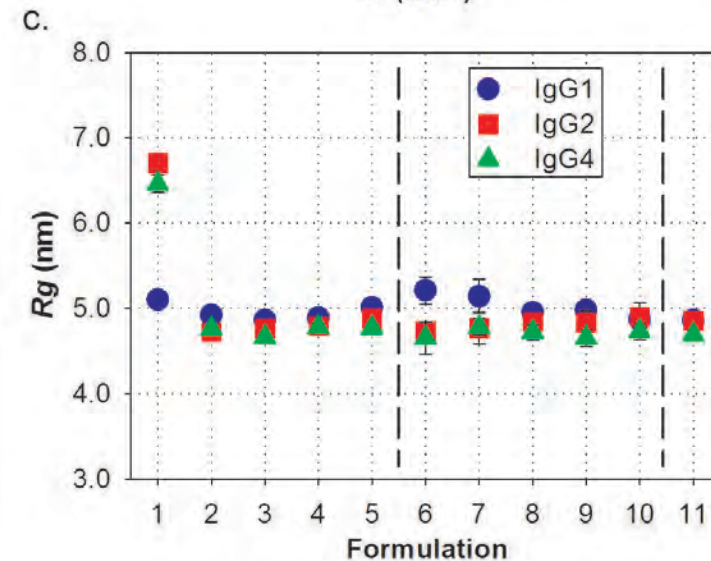
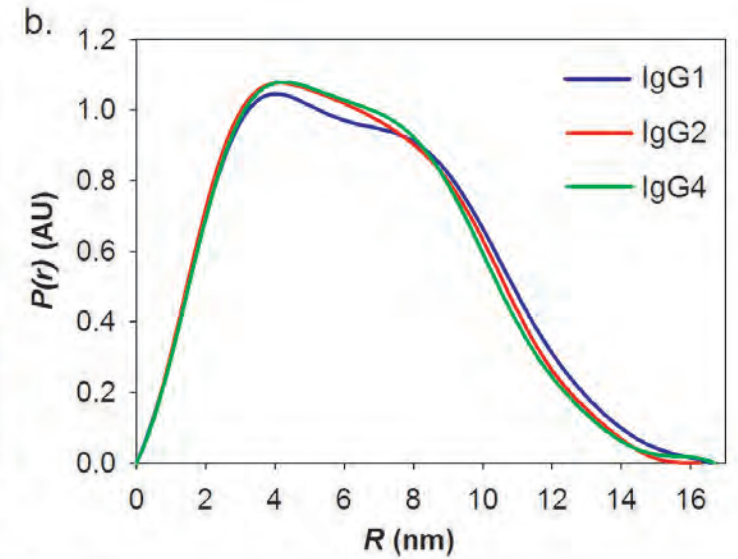
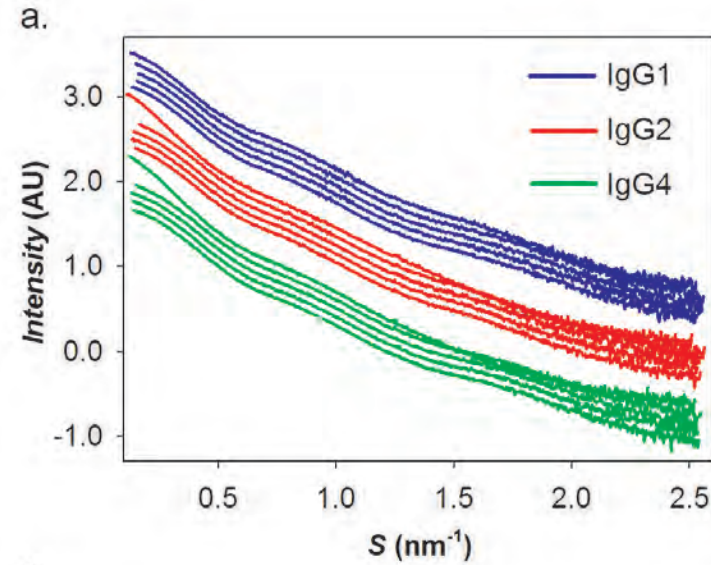
Analysis of IgG subclass structure and aggregation properties



Identical light chains and identical variable regions in the heavy chain

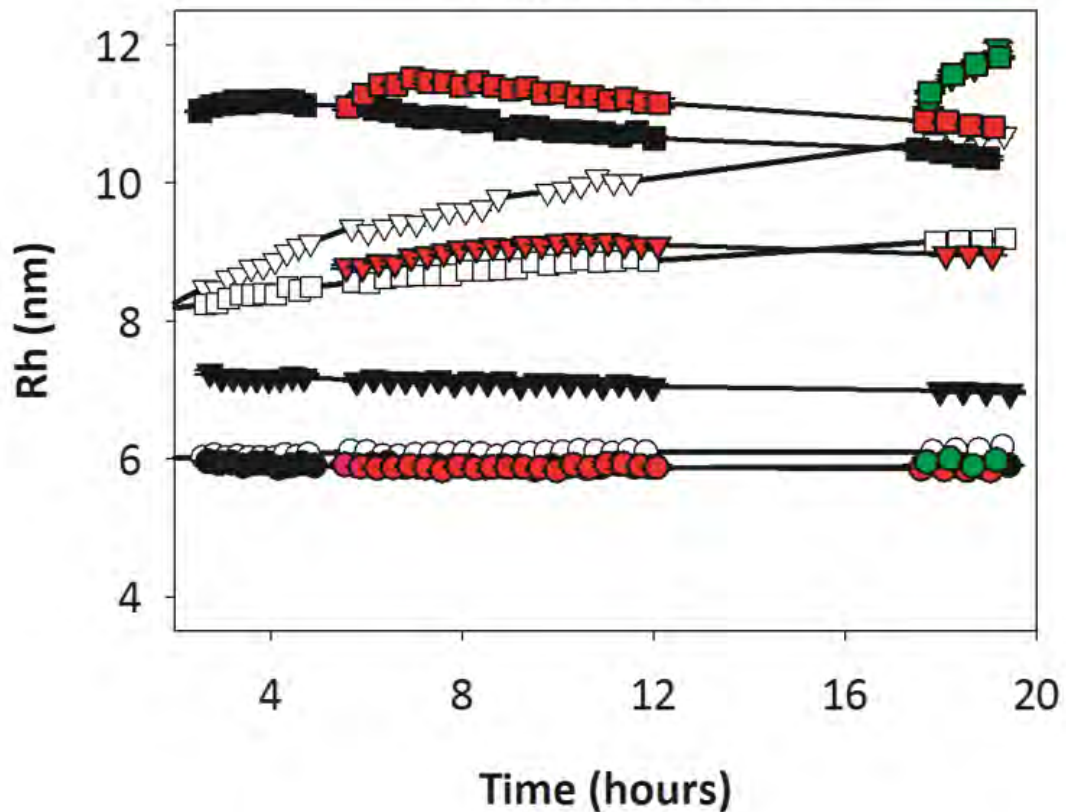


Low-pH: relevant during production of therapeutic antibodies (affinity chromatography and virus deactivation)



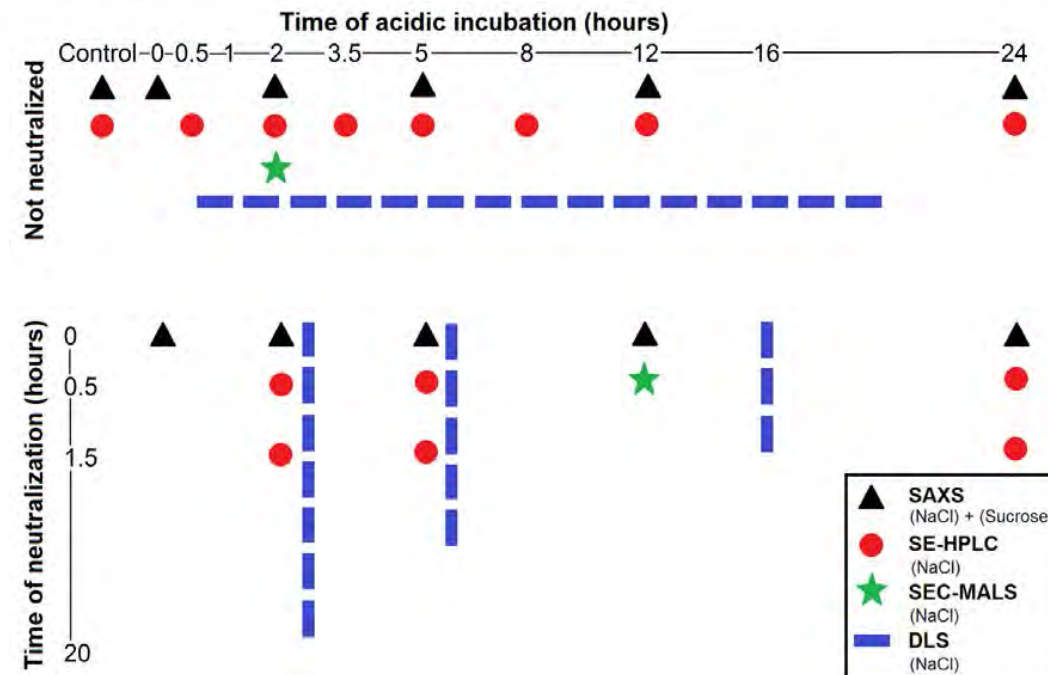
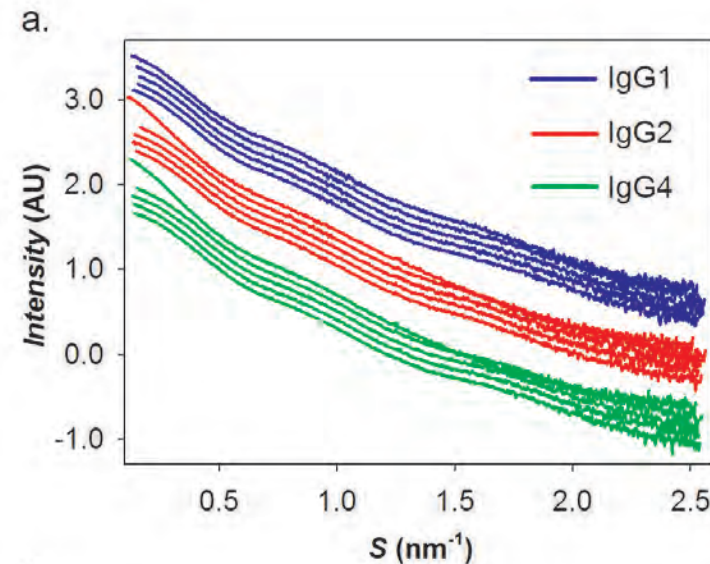
Low-pH induced aggregation study

NaCl, neutralized



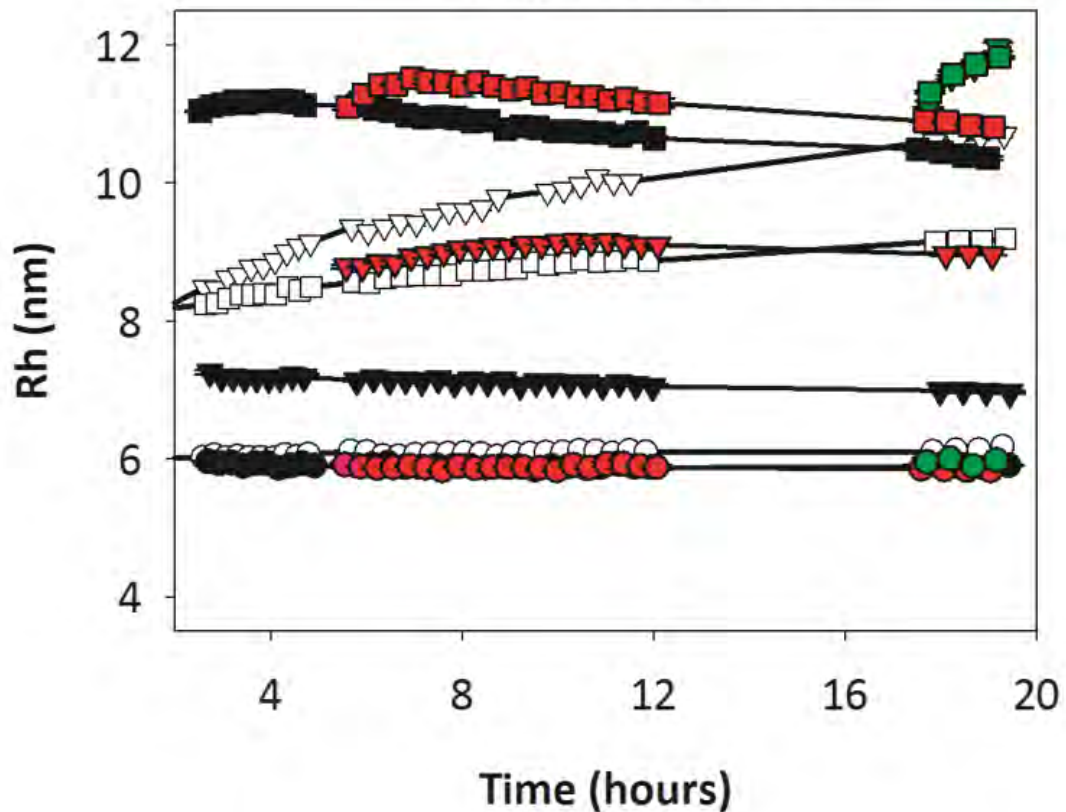
- IgG1
- ▽ IgG2
- IgG4
- 2 hours / neutralized
- 5 hours / neutralized
- 16 hours / neutralized

Low-pH: relevant during production of therapeutic antibodies (affinity chromatography and virus deactivation)

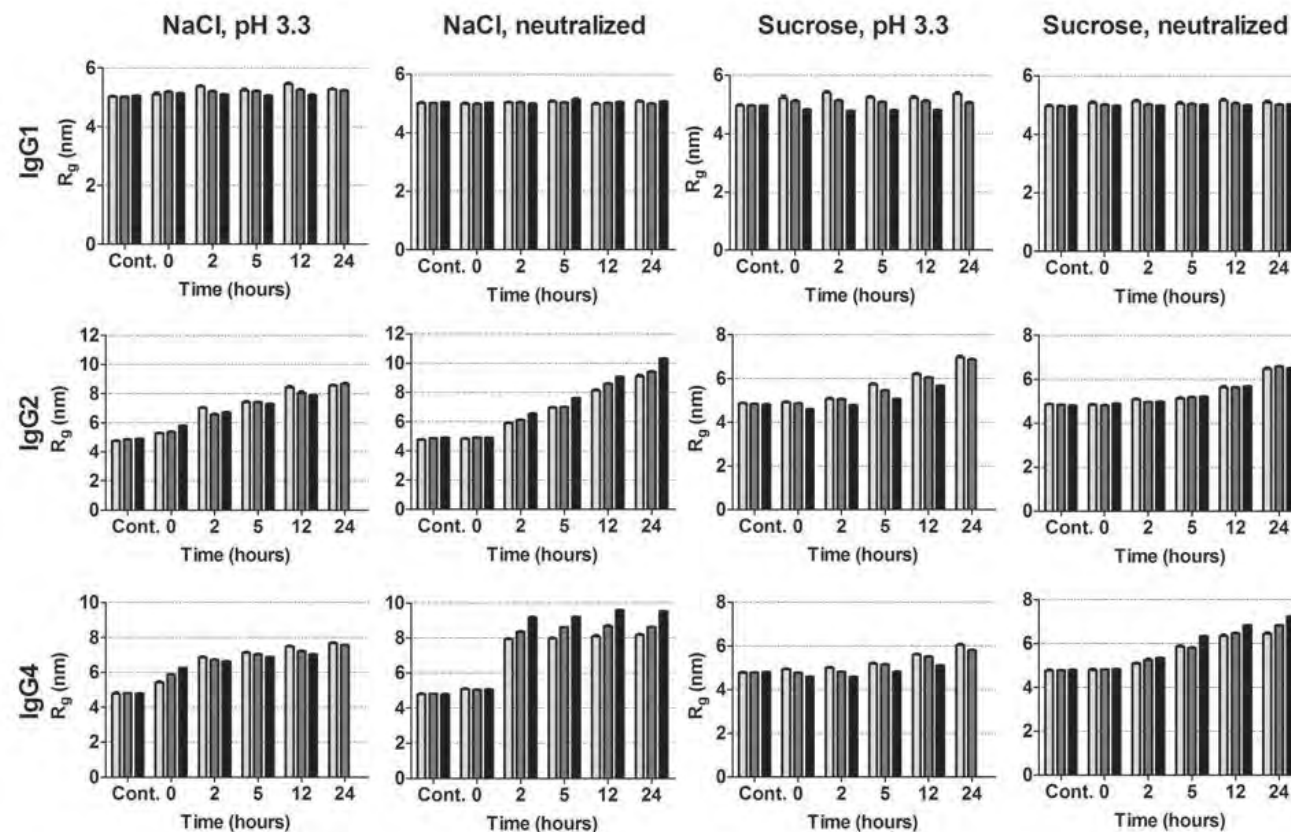
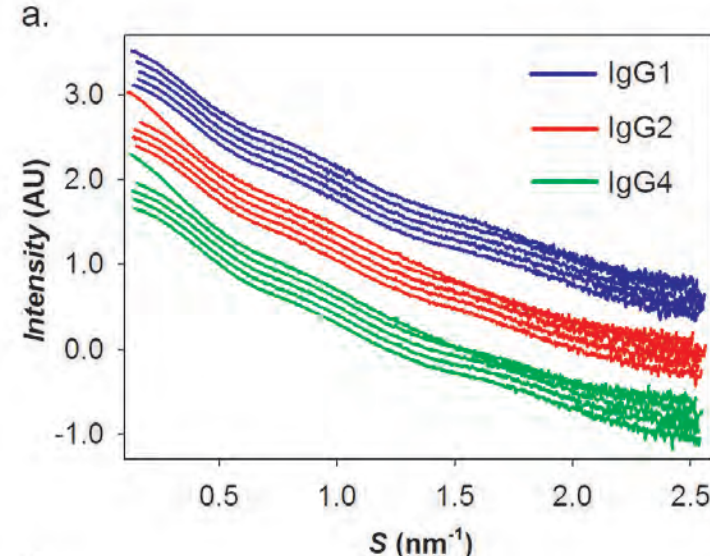


Low-pH induced aggregation study

NaCl, neutralized

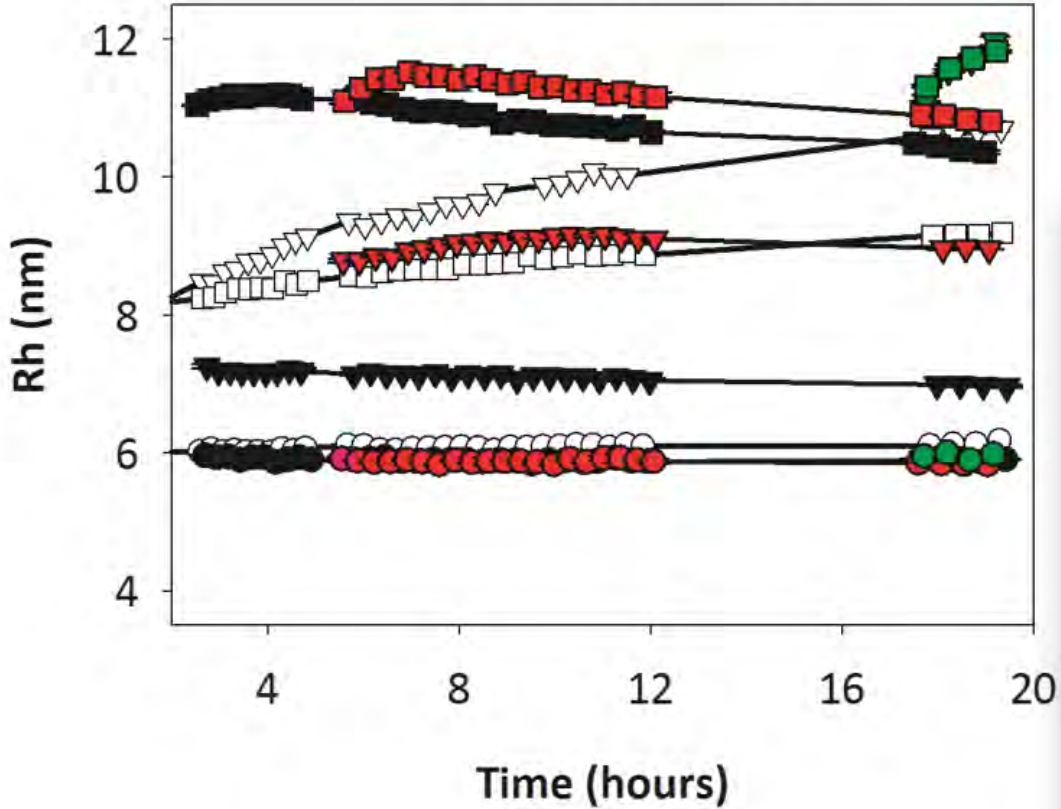


Low-pH: relevant during production of therapeutic antibodies (affinity chromatography and virus deactivation)

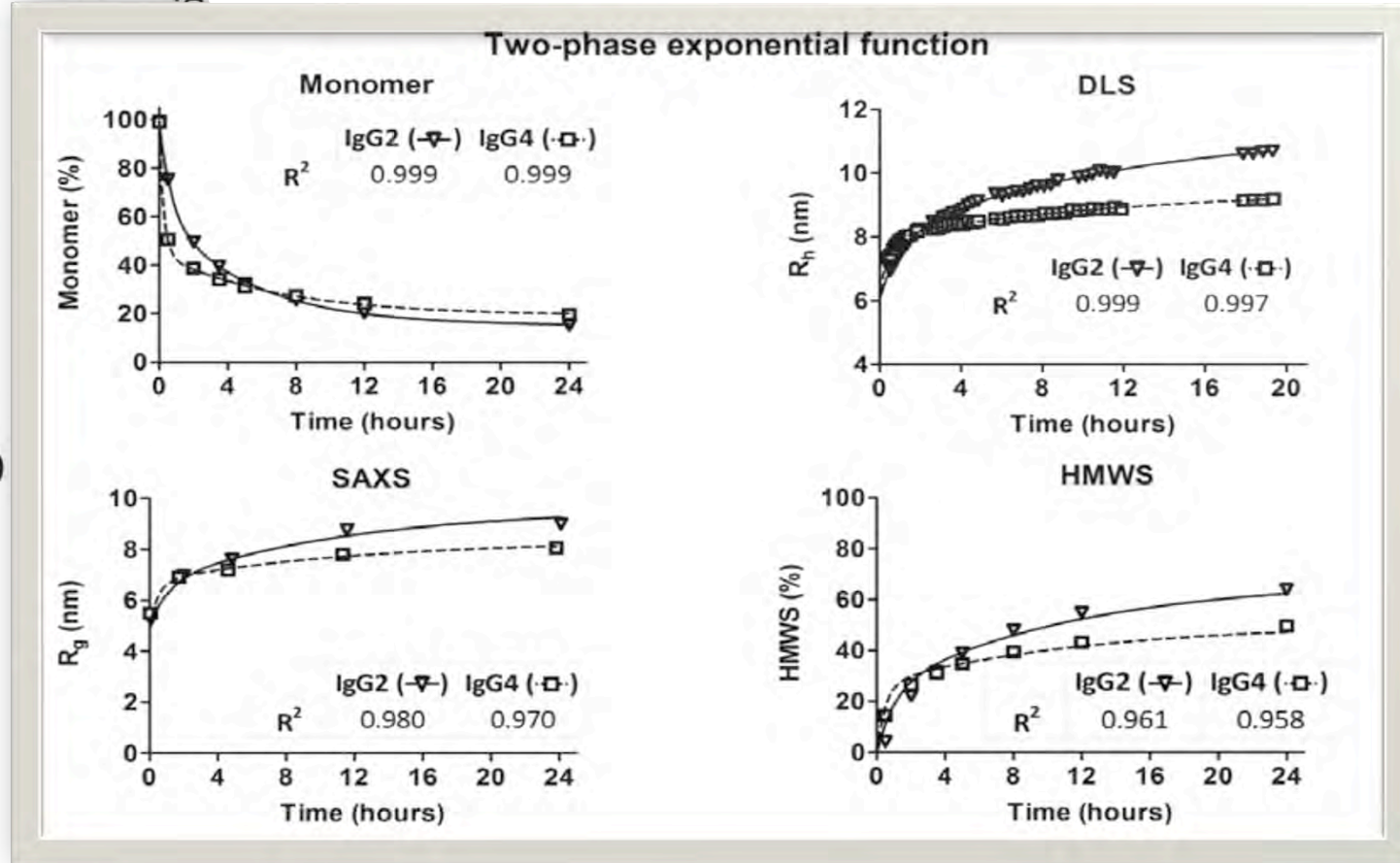
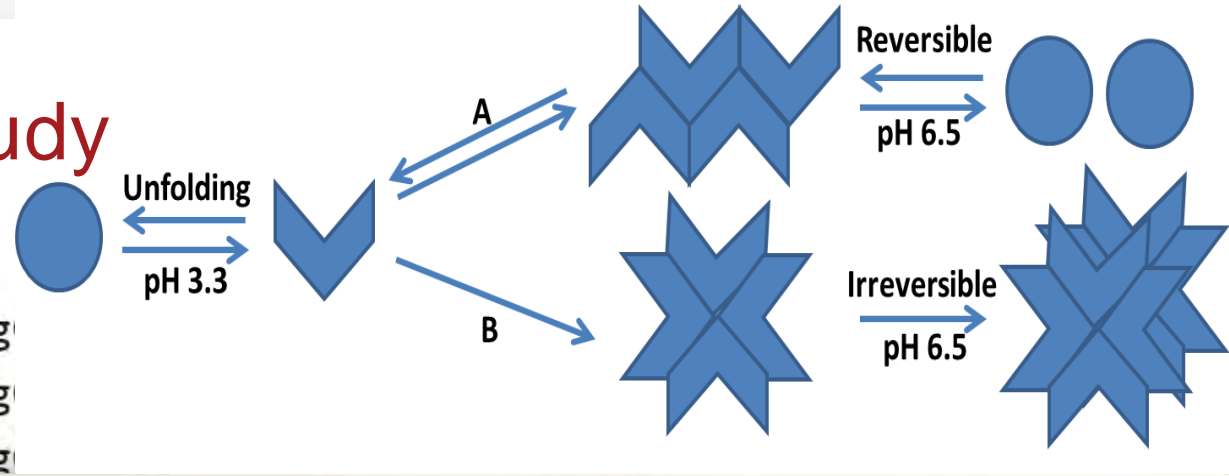


Low-pH induced aggregation study

NaCl, neutralized



Low-pH: relevant during production of therapeutic antibodies (affinity chromatography and virus deactivation)



Acknowledgements:

EMBO @ Suwon organizers

Slides/notes: Vito Foderà, Lise Arleth, University of Copenhagen

Further reading: Notes from Lars Øgendahl, University of Copenhagen

Thank you for your attention

Questions?

http://igm.fys.ku.dk/~lho/personal/lho/lightscattering_theory_and_practice.pdf

Results presented:

ConA aggregation: Valeria Vetri & Maurizio Leone, University of Palermo; Vito Foderà, University of Copenhagen

Insulin analogue oligomerisation: Malene H. Jensen & Marco van de Weert, University of Copenhagen; Per-Olof Wahlund, Dorte B. Steensgaard, Jes K. Jacobsen & Svend Havelund, Novo Nordisk A/S

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